# بَ0 <br> UNIVERSIDAD REY JUAN CARLOS 

# INGENIERÍA DE TELECOMUNICACIÓN INGENIERÍA TECNICA EN INFORMÁTICA DE SISTEMAS 

Curso Académico 2014/2015

Proyecto Fin de Carrera

## ENERGY HARVESTING FROM MOVEMENT

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La defensa del presente Proyecto Fin de Carrera se realizó el día de de 2015, siendo calificada por el siguiente tribunal:

Presidente:

Secretario:

Vocal:
y habiendo obtenido la siguiente calificación:

Calificación:

Dedicate to
all people who supported me and believed in me

## Acknowledgments

Los agradecimientos será la única parte en español del proyecto porque es muy difícil expresar todo lo que siento en otro idioma.

Quiero darle las gracias a mis padres, Pedro y Amparo, a mi hermana, Andrea y a mi abuela Esperanza, porque sin su apoyo, su fuerza no habría sido capaz de llegar hasta aquí. También tengo muchísimo que agradecer a Ana, mi novia, por soportar todo este curso a mi lado incluyendo estrés, nervios y enfados que ha generado este ultimo curso de carrera tan estresante. A Joshua y Pablo porque siempre están ahi cuando necesito echar unas risas, unas cervezas o lo que haga falta.

Me gustaría también agradecer a todos los compañeros que me han acompañado y ayudado en la carrera. Quiero hacer especial mención a Carlos porque que seria de Polonia sin ese gran año juntos y todo lo que paso es un trocito muy importante en mi vida ya lo sabes. A Joel por tantas cosas que me aportas en el día a día siempre apoyando en todo y haciendo reír a todo el mundo eres genial. A Franco porque es el mejor "basketcista" de toda europa y mejor persona, y aporta el punto de seriedad que muchas veces me ha hecho falta. Raquel, gracias por todas las charlas que he tenido de tantas cosas contigo. Peligros por estar siempre ahi aunque estemos lejos y quiero agradecer también a Macarena por toda la fuerza que durante este curso me ha dado para seguir luchando.

Quiero hacer un aparte a la gente que he conocido en Polonia desde Cesar,Anabel, Moni, Justyna, Marcin, Aldona, Pablo, Guillaume... Porque me han aportado muchísimas cosas y me han ayudado a que la adaptación al nuevo país sea inmejorable y me sienta genial cada día en Cracovia.

En definitiva quiero agradecer a todos por estar a mi lado por darme lo mejor y por estar de una forma $u$ otra en mi vida. Os quiero.

Por ultimo, gracias a Gregorio Robles por facilitarme la realización del proyecto a
distancia y por ayudarme a realizarlo de la mejor manera no se me ocurre otro profesor que me hubiera ayudado mejor.

Y para acabar serdecznie dziekuje Doktorowi Piotrowi Dziurdzia za pomoc udzielona nie tylko przy tym projekcie, ale w ciagu calego roku.

Muchas gracias a todos

## Summary

Energy is wasted everyday in every place and nowadays is really important the use of green energy or renewable energy. Parallel to this type of energy, appeared few years ago the concept of energy harvesting, which has a lot of different types and applications.

This thesis is based on the study of energy harvesting on the move. Energy harvesting is the use of energy that is wasted each day. In recent years there have been many experiments related to this topic and this is one more. Among the different types of possible ways to take this energy I have selected one of them which is electromagnetism.

The main objective of my thesis is the search for a prototype to charge the battery of your own device whether smartphone, bike-pc or anything else. Currently the batteries are less durable and in a few hours you have to charge them to carry on working with them, thanks to the movement that I made in our bike these batteries could be charged during our journey on the bicycle.

During the process of my thesis I have researched on energy requirements and systems that could the prototype need for the las target. I used circuit simulation tools such as LTSpice and I also installed a prototype of bicycle in the laboratory to manage with all the testing needed.

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## Chapter 1

## Introduction

"To convince people to back your idea, you've got to sell it to yourself and know when it's the moment. Sometimes that means waiting. It's like surfing. You don't create energy, you just harvest energy already out there."

In this chapter I will make a brief introduction of this final project. Explain the motivation that led us to realize as well as the goals I want to achieve. Also expose the memory structure of a short form to put in situation the reader of what will be found throughout the following chapters.

The purpose of this Final Project to be understood and improve the way in which I waste energy, such as the energy that is lost in the movements, body temperature...

For this reason I decided to get involved with energy harvesting looking for a project that could exploit the energy to so I can improve the utilization of this lost energy. At first I choose to orient toward the human body or something more electronic finally decided to get involved in the simulation, creation and optimization this prototype autonomous charger on a bicycle.

### 1.1 Context

The increase of energy consumption, has created the need to implement new methods of harvesting, conserving and optimally using energy. Movement in devices wheels, motor... is just one example of the multitude of untapped energy source on everyday life, that can be used to get amount of energy. Developing methods to harvest energy from
these movements is a particular challenge, because there is a lot of applications for these methods.

Movement of wheels provides excellent case-study to explore the energy harvesting related with magnetic fields. In present day there is no way to get energy on bike for bike-computer, GPS... A solution to these inconveniences would be a circuit that can get energy from the movement of the bike for the devices.

### 1.2 Motivation

it all started when speaking with my tutor in Poland, he commented to me about the research he has being conducted. Dr. Dziurdzia sent me several articles based on energy harvesting and I was very interesting on the topic from the first sentences I read about it. I started researching about this fear and finally chose energy harvesting with electromagnetic fields.

### 1.3 Objectives

The goal of this thesis is to create models to serve as a designs aid and optimization tool for system that harvest energy from movement.

The focus of this thesis is to prove the feasibility of such a system and document the creation of a proof-of-concept prototype.

### 1.4 Structure

In Chapter 2 of this thesis I will describe what is Energy Harvesting, which are the most commonly used methods and the different magnetic harvesting that exists.

During Chapter 3 I will make a brief explanation about which are the different technologies I use during the thesis.

On Chapter 4 I will explain all the main process I have done for this thesis. Firstly I will describe the simulation I did using LTSpice software and why I change the simulations few times. Also, I will explain the different Integrated circuit I can use for my thesis and
which it is the most suitable for my target.
Finally in chapter 5 and 6 it will be shown the results and conclusion about the thesis.

## Chapter 2

## Energy harvesting

Energy harvesting is possible to implemented in different ways. Calculate the energy requirements of an applications is really important to select the appropriate energy harvesting strategy. This chapter discusses the energy requirements of the bicycle and the selection of an energy harvesting strategy to meet these specifications. The whole theoretical calculations and formulas will be on Appendix A.

### 2.1 Energy Requirements

Firstly is necessary to identify the energy requirements of the system and determining if the energy harvesting is a viable approach to satisfy them. The energy requirements for our objective are specified in terms of power budget. The current system of energy harvesting in bicycle is the dynamo. The new efficient system will provide the rider the chance to have a charger on his bike. The power requirement for a charger is around 3.3 V .

### 2.2 Energy Requirements Systems

There are many ways of harvesting energy from vibrations. Three of the most common methods are: Variable Capacitance Systems, Piezoelectric Material Systems, and Magnetic Induction Systems. Each of these will be studied and their typical power outputs evaluated. Table 2.1 shows a comparison table of the three options.

### 2.2.1 Variable Capacitance Systems

Variable capacitance systems employ parallel-plate capacitors with movable plates. The plates are charged to a specified voltage. The plates are then mechanically moved apart by the input vibrations. Increasing the distance between the plates causes energy to be stored in the capacitor.

This energy can be harvested when the plates are brought closer to each other again. The magnitude of energy that can be harvested from such systems is generally on the order of micro watts.

### 2.2.2 Piezoelectric Material Systems

Piezoelectric materials build up a voltage differential across their ends when they are subjected to mechanical deformation. When energy from vibrations is harnessed to cause deformation in such materials, the voltage difference generated can be used to charge a capacitor or other energy-storage device. The magnitude of energy harvested from piezoelectric systems can vary from micro watts to watts.

### 2.2.3 Magnetic Induction Systems

Magnetic induction systems generate power through relative motion between a coil of wire and a magnet. This causes the magnetic flux through the coil to change, which leads the generation of a voltage differential across the ends of the wire coil. This voltage difference can be used to charge a capacitor or other energy-storage device. The magnitude of energy harvested from magnetic induction systems can range up to kilowatts depending on the size of the system.

|  | Variable Capacitance | Piezo Material | Magnetic Induction |
| :---: | :---: | :---: | :---: |
| Power generation | $\mu \mathrm{W}$ | $\mu \mathrm{W}-\mathrm{W}$ | $\mathrm{mW}-\mathrm{kW}$ |
| Vibration amplitude | $\mu \mathrm{m}$ | $\mu$-m | $\mathrm{mm}-\mathrm{cm}$ |
| Driving frequency | Any range | Tens of Hz | Any range |
| Ease of system design | Difficult | Easy | Easy |
| Cost | High | High | Modest |
| Lifetime | Low | High | High |

Table 2.1: Comparison of energy harvesting strategies.

### 2.3 Magnetic Induction System Design

Magnetic induction systems generate power through relative motion between a coil of wire and a magnet. The result of this is the magnetic flux through the coil to change, which leads the generation of a voltage differential across the ends of the wire coil. This voltage difference can be used to charge a energy-storage device. The magnitude of energy harvested from magnetic induction systems can range up to kilowatts depending on the size of the system. The comparison table (Table 2.1) shows this to be the most costeffective and promising option for our experiment.

The power that can be harvested by a magnetic induction system depends on many things, including the size and geometric configuration, the magnetic flux density of the magnets, the number of turns of wire in the coil, and the excitation frequency. There are two magnetic induction systems - magnet-through-coil and magnet-across-coils - in order to enable an understanding of how these systems can be designed and optimized for specific applications, this methods will be evaluate.

The objective of analyzing these magnetic induction systems is to calculate their output voltage and power, this parameters are the most interesting one in the project.

Firstly is necessary to calculate the magnetic field, $H$, in the system. The magnetic field gives the magnitude of magnetic flux density, $B$, and hence the magnetic flux, $A$, through the coils. Once the flux through the coils is known, the open-circuit voltage across them, $V$, can be calculated using Faraday's Law. Ohm's Law and Kirchhoff's Laws are
then used to determine the average power, $P$, dissipated through a load resistor attached to the system. Figure 2.1 shows a flowchart of the steps involved in the analysis of magnetic induction systems.


Figure 2.1: Flowchart of steps

### 2.3.1 Magnet-through-coil Induction

Description of the governing equations for voltage generate by a magnet through a coil. The advantage of this system is the easy way to build it; the disadvantage that the flux reversal of the coil never is complete, and the voltage and power is low. The most common example is a shaker flashlight. The device is powered by the movement of a magnetic relative to a coil when is shaken.

The magnet-through-coil induction system consists of a cylindrical coil that translates relative to a bar magnet of height $l_{m}$ and radius $r_{m}$. The longitudinal axis of the magnet is set along the y-axis, with its midpoint at the origin. The coil, made of $N$ turns of wire, has height $I_{c}$, inner diameter $d_{m}$ in and outer diameter $d_{m} a x$. The average radius of the coil, $r_{c}$, is calculated as:

$$
\begin{equation*}
r_{c}=\frac{d_{\min }+d_{\max }}{4} \tag{2.1}
\end{equation*}
$$

The average diameter of the coil, $d_{c}$, is $2 r_{c}$. The cross sectional area of the coil, $A_{c}$, is
calculated as

$$
\begin{equation*}
A_{c}=\pi r_{c}^{2} \tag{2.2}
\end{equation*}
$$

The magnet is fixed in place while the coil moves along the y -axis. The y -coordinate of the lower end of the coil is defined as $h$. The coil is assumed to vibrate with a fixed amplitude, $a$, at a single frequency, $f$, with the motion centered at the y-coordinate dc. Figure 2.2 shows the labeled geometry of this system.


Figure 2.2: A cross-sectional view of the magnet-through-coil induction system.

### 2.3.2 Magnet-across-coils Induction

The magnets-across-coils induction system consists of a layer of magnets separated by an air gap from a layer of coils. The magnets move across the coils, causing a change in magnetic flux and generating a voltage across the coil ends. The system has three phases: A, B and C. Figure 2.3 shows a schematic of the system to be analyzed.

Since the permeability of a magnetic material like steel is typically orders of magnitude higher than that of air, the magnetic backing for the coils and magnets is assumed to have infinite permeability. The now simplified problem is to solve for the magnetic fields in the gap between the two layers of magnetically permeable material, where magnetic fields are generated by the magnets and by coil current.

As all the elements of the system are linear, the fields due to the magnets and coils can each be calculated separately and then added by superposition. This breaks the problem into three smaller tasks: (1) calculation of the magnetic field due to the magnets; (2) calculation of the fields due to the flow of current in the coils; and (3) adding them by superposition and finding the total voltage and power generated.


Figure 2.3: Magnet-across-coils induction system

## Chapter 3

## State of the art

This chapter aims to give an overview of the technical and technological tools that have been taken into account during this project. In this chapter the technologies are presented, in the next chapter is shown how have been used in this project.

For the preparation of this chapter has been used by multiple sources, mainly web pages, books and articles. All are properly referenced.

### 3.1 LTspice

LTspice $~^{1}$ is a high performance SPICE simulator, schematic capture and waveform viewer with enhancements and models for easing the simulation of switching regulators. Our enhancements to SPICE have made simulating switching regulators extremely fast compared to normal SPICE simulators, allowing the user to view waveforms for most switching regulators in just a few minutes. Included in this download are LTspice IV, Macro Models for $80 \%$ of Linear Technology's switching regulators, over 200 op amp models, as well as resistors, transistors and MOSFET models.

[^0]

Figure 3.1: LTspice circuit Example

### 3.2 Altium Designer

Altium Designer ${ }^{[2}$ is an electronic design automation software package for printed circuit board, FPGA and embedded software design, and associated library and release management automation. it is developed and marketed by Altium Limited of Australia.


Figure 3.2: Eagle Board Example

[^1]
## Chapter 4

## Design and Implementation

This chapter explains the design of the prototype of my thesis, and also the changes that I have made in this prototype during the time. At the same time of the design, are shown corresponding simulations with the design state at that time.

### 4.1 Prototype components

This section describes the different kinds of components which are necessary to implement the final set-up of the laboratory.

### 4.1.1 Motor

A motor is an electrical machine that converts the electrical energy into mechanical energy. There are tow different kinds of motors, DC and AC. In our case DC motor is the one used on the prototype. The DC motor gets the electrical energy from a Power Supply.


Figure 4.1: Different motors

### 4.1.2 Roller

it is a component designed to roll, in the project it is related to the movement of the DC motor shaft.

### 4.1.3 Wheel

it is a circular component that has rotates on an axial bearing. A bicycle wheel, most commonly a wire wheel,is one wheel designed for a bicycle. A pair is often called a wheelset. A typical modern wheel has a metal hub, wire tension spokes and a metal or carbon fiber rim which holds a pneumatic rubber tire.


Figure 4.2: Bicycle wheel

### 4.1.4 Holder

The holder is the part where all the rest of the prototype is attached to with screws, glue or different fastening methods.

### 4.1.5 Tachometer

A tachometer is an instrument to measure the rotation speed of shaft, disk or more. Normally these devices shows Revolutions per minute (RPM) on an analog dial, but nowadays also are common the digital ones.


Figure 4.3: Tachometer

### 4.1.6 Magnets

Magnet is a material or object than can generate magnetic fields. This field generates a force that pulls from some material and attracts others.


Figure 4.4: Magnets

### 4.1.7 Coil

A coil is an electrical conductor like a wire in spiral or helix. Electromagnetic coils are used, in applications where electric currents produce magnetic fields, in devices like inducts, electromagnets, transformers...


Figure 4.5: Coils

### 4.1.8 Transformers

A transformer is an electrical device that transfers energy between two or more circuits through electromagnetic induction. Commonly, transformers are used to increase or decrease the voltages of alternating current in electric power applications.


Figure 4.6: transformers

### 4.1.9 Integrated Circuits

An integrated circuit is a joint of circuits on a chip of semiconductor material. This is smaller than a typical circuit, it has a lot of transistors and other components and is not much bigger than a fingerprint.


Figure 4.7: integrated circuits

### 4.1.10 Components for IC

Capacitors and resistor are electrical components needed on the IC circuit.

### 4.2 Uses of components of the prototype

### 4.2.1 Motor

In the prototype, a motor is arranged to generate the movement that would be generated by a person pedlling the bicycle. This movement is the mechanical energy that the DC motor generates on the shaft by the rotation of this part.


Figure 4.8: DC motor

### 4.2.2 Roller

In Figure 4.8 it is possible to see that there is a roller to move the wheel in a better way, because the DC motor generates a movement that can?t move the wheel with the shaft. In order to have a good movement of the wheel, it was prepared like this the DC motor with this roller.


Figure 4.9: Roller

### 4.2.3 Wheel

it is the main part of the prototype which will move and generate the magnetic field. This movement is produced by the whole set of the DC Motor and Roller.


Figure 4.10: Wheel of the prototype

### 4.2.4 Tachometer

The tachometer will get the value of the RPM of the wheel. To use the tachometer it is necessary to have a small reflective material on the wheel.


Figure 4.11: Tachometer

### 4.2.5 Magnets

The magnets will be distributed around the rim to produce a constant magnetic field. They are one of the important parts of the prototype to generate our final voltage.


Figure 4.12: Magnets on the wheel

### 4.2.6 Coil

The coil will be established closed to the rim of the bicycle. The coil will generate electrical energy because of the movement of the magnets. First I used coils that I can have on the market like the one on Figure 4.13 and also figure 4.14.


Figure 4.13: First coil


Figure 4.14: Second coil

Finally I decided to create our own coil. I create this coil with a wire of 0.5 millimeter of thickness, and with 100 round.


Figure 4.15: Costume coil

Inside the coil from Figure 4.15 I put inside some ferromagnetic as is shown in the Figure 4.16.


Figure 4.16: Ferromagnetic Material

### 4.2.7 Transformers

The use of the transformers in the prototype its really important because they will increase the value of the voltage obtained on the coil to a necessary voltage for properly operation of the IC.


Figure 4.17: Different Transformers

### 4.2.8 Integrated Circuits

The integrated circuits are circuits focused on energy harvesting that can convert a really slow voltage into one enough to charge a battery.

### 4.3 Design and simulation history

The first step in the project, was to mount the prototype for the laboratory and set up everything (dc motor, wheel, holder, roller) to start getting some values. This first part it is really important because it is useful to know the range of voltage I will have on the prototype.


Figure 4.18: First prototype

With the first range of voltage's value I was able to perform a simulation on LTSpice based on LTC3108 converter. Firstly the simulation with the converter was focused on obtaining in which range I can start simulating, so I decided to have the same configuration of the circuit changing the values of the voltage 3 V or 5 V and changing the frequency of the $V_{i n}{ }^{1}$ At this moment I was just checking which IC would be more suitable for my prototype, so looking at data sheet of LTC310 $\mathbb{Z}^{2}$, it is possible to verify the different kinds of applications.


Figure 4.19: Simulation circuit 1

As it can be verified on the data sheet the first configuration was wrong. It is not necessary to connect $C_{2}$ to SW and also the values of the capacitor are not correct. So as I can see in Figure 4.19 I took out the battery because I didn't need it for the simulation. Just getting the right value at the $V_{\text {out }}$ would be perfect to achieve my target.

[^2]

Figure 4.20: Simulation circuit 2

At the same time I was working on the simulation with LTSpice, I was working to improve the prototype with different coils to generate more voltage and also to get a more stable voltage. Finally I decided to create my own coil ${ }^{3}$ and I attached the coil to the holder of my prototype to keep it stable and close to the rim of the wheel.


Figure 4.21: Homemade coil attached to the prototype

[^3]The next modification in the simulation circuit was to attach a transformer just to get a greater value of the $V_{i n}$ in the converter, because I realized that the voltage with the higher speed it was around 1.1 V . So the next changes in the circuit were related to the different ratio of the transformer 1:20, 1:50 or 1:100.


Figure 4.22: Simulation circuit ratio 1:20


Figure 4.23: Simulation circuit ratio 1:100

At this part of the project my tutor told me to take a look also at LTC3109 as it could be suitable for my objective. So taking a look at the data-sheet $t^{4}$ I prepared a simulation for this new IC than could be used in with the prototype.

[^4]

Figure 4.24: Simulation with LTC3109

With this simulation there were some troubles on the $V_{\text {out }}$ values and it was necessary to attach a resistor on the negative part of $V_{i n}$ as is shown in Figure 4.24.


Figure 4.25: Simulation with LTC3109 and resistor

After this point the simulation of my circuits in LTSpice are finished and I was able to start with the simulation of the PCB board that I would use on my prototype. So, first of all I needed to create a necessary scheme of the whole circuit with all the connections from the IC to the output and also create a model of how I weld all components in the PCB board. On the figures below is shown both the scheme and the model for each IC LTC3108 and LTC3109, for this issue I used the Altium Designer.


Figure 4.26: Scheme of LTC3108 circuit


Figure 4.27: Welding simulation LTC3108 circuit


Figure 4.28: Scheme of LTC3109 circuit


Figure 4.29: Welding simulation LTC3109 circuit

## Chapter 5

## Results

In this chapter I will describe and discuss all the results form the simulation and after this the results from the prototype. I will reference all the time to the Section 4.3 Design and simulation history.

At the first part of the results, I started with the simulation circuit from Figure 4.18. I got two values of input voltage ( 3 V and 5 V ) and I also changed the frequency of $V_{i n}$ to get how this change of the frequency affects to my circuit.


Figure 5.1: Simulation LTC3108 values:3V 10Hz


Figure 5.2: Simulation LTC3108 values: 3V 60Hz


Figure 5.3: Simulation LTC3108 values: 3V 100Hz


Figure 5.4: Simulation LTC3108 values: 5 V 10 Hz


Figure 5.5: Simulation LTC3108 values: 5V 100Hz

It was possible to observe some errors in this simulation. First when I looked again in the data sheet of 3108 I knew that it was not necessary to connect $C_{2}$ to SW. So I changed it as we can see on Figure 4.19.

Second, as it was possible to see $V_{\text {out }}$ couldn't reach the expected value to charge a battery. This value has to be 3.3 V and in the first simulation the graph for $V_{\text {out }}$ reached 2.2 V . To fix this problem I noticed that the connection of $C_{3}$ didn't exist as I can see there is no a dot in the wire that means there is no connection. Thats why I got in $V_{\text {out }}$ 2.35 V instead of 3.3 V .

Third, there was no change if I increased or decreased the frequency of the $V_{i n}$. I obtained the same values for each frequency $10 \mathrm{~Hz}, 60 \mathrm{~Hz}$ or 100 Hz . So for the next simulation it was not important which frequency I would use to simulate the circuit.

On the other hand, I prepared my homemade coil. I decided to do it like this because with this method I was able to decide all the specifications of my coil.

|  | Homemade Coil |
| :---: | :---: |
| Wire Thickness | $0,5 \mathrm{~mm} \mathrm{~W}$ |
| Bounds | 100 |
| Length | 7 cm |
| Internal Resistance | $3,5 \Omega$ |
| Inductance without Ferromagnetic's | $0,54 \mathrm{mH}$ |
| Inductance with Ferromagnetic's | $9,2 \mathrm{mH}$ |

Table 5.1: Homemade Coil Values

As it is possible to see on Figure 4.20, I attached the coil to my prototype and I did some tests on the prototype because it was the last change on the laboratory prototype. This part of the project was really important, I got a range of Voltage in the output of the homemade coil from 0.3 V to 1.1 V .

This testing changed the whole simulation because I was simulating with a wrong range. Also, I needed to change the value of $R_{1}$.

Because of this change in the range of voltage it was necessary to attach a transformer between the coil and the input of LTC3108. It was necessary to increase the value that goes to the IC because now the maximum value $V_{i n}$ it wasn't enough for the IC input.

As it is possible to see on the Figure 5.6 after attaching the transformer, I was able to improve the voltage value ( $V_{1}=$ voltage before transformer $V_{2}=$ voltage after transformer) that would be the input to the IC.


Figure 5.6: Comparison of $V_{1}$ ande $V_{2}$

Now I had to check how the differences rates of the impedance of the transformer, that
are possible to get in the market, and how this will affect to the result. In Figure 5.7, 5.8, 5.9 and 5.10 it is possible to discard this simulation because there is no difference when I change the values of the impedance.


Figure 5.7: Circuit with transformer of $2,5 \mathrm{H}$


Figure 5.8: Circuit with transformer of 3 H


Figure 5.9: Circuit with transformer of 4H


Figure 5.10: Circuit with transformer of 5 H

The following step is to test if it is required to include a rectifier circuit on the input to have positive values of the signal or just positive and 0 value all the time. In Figure
5.11 and 5.12 there is a scheme of the simulation, where I included a capacitor, resistor and a diode.

Also, I tried this kind of rectifier without resistor to see the difference. This circuit is a rectifier of half wave, this means that the negative part will be 0 . I made some simulation with a 4 diode bridge that would rectify the whole wave, which gave me positive value of the signal in the total time. I don't include the Figures of the bridge because there was no result on the $V_{\text {out }}$ with such a circuit.


Figure 5.11: Half Wave Rectifier Circuit 1


Figure 5.12: Half Wave Rectifier Circuit 2


Figure 5.13: Half Wave Rectifier Circuit 5


Figure 5.14: Half Wave Rectifier Circuit 4

The rectifier circuit doesn't work well on this IC circuit in 10 second $V_{\text {out }}$ doesn't reach the expected 3.3 V . Because the operation configuration of the LTC3108 is in Charge Pump and Rectifier mode. So I can conclude that it is not necessary to apply a rectifier circuit, because the IC do this part of the problem.

At this moment I have a good configuration of LTC3108 that can be used for the prototype. I was requested from my tutor to take a look also at LTC3109, so I started some simulation with this IC. In the circuit from Figure 4.24 there was no result on $V_{\text {out }}$. With these simulations of LTC3109 I had big problems due to the duration of the simulations, which took between three or four days to simulate 5 seconds. This is the reason why from this point I only had few simulation of LTC3109.

Then, I realized that i needed to attach a big resistor in the circuit as it is shown on Figure 4.25. Also due to the length of the simulations they were not conducted until 3.3 V in $V_{\text {out }}$ is obtained, it is understood that when $V_{l d o}$ manages to obtain a high value within a reasonable time, $V_{\text {out }}$ will reach the expected value of 3.3 V .

|  | LTC3108 circuit |
| :---: | :---: |
| Transformer ratio | $1: 100$ |
| $C_{1}$ | $2,2 \mu \mathrm{~F}$ |
| $C_{2}$ | 1 n F |
| $C_{3}$ | 470 p F |
| $C_{4}$ | $1 \mu \mathrm{~F}$ |
| $C_{5}$ | $10 \mu \mathrm{~F}$ |
| $C_{6}$ | $10 \mu \mathrm{~F}$ |

Table 5.2: LTC3108 Values

|  | LTC3109 circuit |
| :---: | :---: |
| Transformer ratio 1 | $1: 100$ |
| Transformer ratio 2 | $1: 100$ |
| $C_{1}$ | 1 n F |
| $C_{2}$ | 470 p F |
| $C_{3}$ | $10 \mu \mathrm{~F}$ |
| $C_{4}$ | $10 \mu \mathrm{~F}$ |
| $C_{5}$ | $2,2 \mu \mathrm{~F}$ |
| $C_{6}$ | $1 \mu \mathrm{~F}$ |
| $C_{7}$ | 1 n F |
| $C_{8}$ | 470 p F |
| $R_{2}$ | $100 \mathrm{M} \Omega$ |

Table 5.3: LTC3109 Values

### 5.1 Final Simulation Results

I started to test both IC with different ranges of voltage on the $V_{i n}$ and with the values of resistor transformer and capacitor shown in Table 5.2 and 5.3.

### 5.1.1 Final Simulation Results for LTC3108



Figure 5.15: $V_{\text {in }}=0,5 \mathrm{~V}$


Figure 5.16: $V_{\text {in }}=0,3 \mathrm{~V}$


Figure 5.17: $V_{\text {in }}=0,2 \mathrm{~V}$


Figure 5.18: $V_{\text {in }}=0,1 \mathrm{~V}$


Figure 5.19: $V_{i n}=50 \mathrm{mV}$

Due to the duration of the simulation, these figures don't show the $V_{\text {out }}$ result but I can guess that from 0.1 V to higher value in small period of time $V_{\text {out }}$ will get 3.3 V . I can conclude that this circuit is valid for simulations in the prototype.

### 5.1.2 Final Simulation Results for LTC3109



Figure 5.20: $V_{\text {in }}=0,5 \mathrm{~V}$


Simulation Time $=47.3981 \mathrm{~ms}$ Transient Analysis $00.9 \%$ done. Simulation Speed: $2.01644 \mu \mathrm{~s} / \mathrm{s}$ inter $=2$ fill-ins: 26
Figure 5.21: $V_{\text {in }}=0,3 \mathrm{~V}$


Figure 5.22: $V_{\text {in }}=0,1 \mathrm{~V}$

Although I have had many problems with simulations due to the time consuming and they were very heavy, I can say that LTC3109 it is a suitable circuit for the target of charging the battery with my prototype.

### 5.1.3 Circuit welding process

At this moment I know that LTC3109 and also LTC3108 can be suitable for my prototype. So now, I need to weld the IC and transformer to a board with all the values from table 5.2. and 5.3. Figure 4.27 and 4.29 will give us guidance of how the circuit will be welded.


Figure 5.23: Welded Top Board for LTC3108

After some test on the prototype with the two welded board I made. I didn't get a huge difference between LTC3018 and LTC3109. Both of them are suitable for our objective to reach the value to charge a battery. As my tutor had a demo-board from Linear (see Figure 5.26) I decided to test the last part of the project with this demo-board.


Figure 5.24: Welded Bottom Board for LTC3108


Figure 5.25: Welded Top Board for LTC3109


Figure 5.26: Welded Bottom Board for LTC3109


Figure 5.27: Linear Demo-Board

In Figure 5.28 is possible to see how the prototype is connected to the demo-board, to the Multimeter and also to the Power supply (which move the DC motor). So finally, I needed to check that $V_{\text {ldo }}$ and $V_{\text {out }}$ reach the expected values (Figure 5.27 and 5.28).


Figure 5.28: Final Laboratory Prototype

After checking the values of $V_{l d o}$ and $V_{\text {out }}$, I apply to $V_{\text {store }}$ a capacitor of 1 mili Farads and with the internal capacitor of the demo-board, I have a total capacitance of 1,22 mili Farads. With this capacitor what I get is that $V_{\text {store }}$ goes up slower and I will be able to calculate how the speed of the wheel will affect to the $V_{\text {store }}$ (see Table 5.4).

| Speed | Time |
| :---: | :---: |
| $31,79 \mathrm{rpm}$ | 484 sec |
| $38,9 \mathrm{rpm}$ | 202 sec |
| $43,7 \mathrm{rpm}$ | 166 sec |
| $48,73 \mathrm{rpm}$ | 150 |
| $53,6 \mathrm{rpm}$ | 1115 sec |
| $63,31 \mathrm{rpm}$ | 101 sec |
| $70,1 \mathrm{rpm}$ | 69 sec |
| $75,8 \mathrm{rpm}$ | 65 sec |
| $81,8 \mathrm{rpm}$ | 55 sec |

Table 5.4: Time from 1 V to 5 V of $V_{\text {store }}$


Figure 5.29: $V_{l d o}$ Value


Figure 5.30: $V_{\text {out }}$ Value

## Chapter 6

## Conclusions

### 6.1 Achievement of objectives

After all the research about Energy Harvesting, simulation with LTSpice and the subsequent testing of the prototype, it can be said that the objectives have been achieved. Finally the circuit I made reached the expected value for charging the battery at the output.

The time to reach the output value it is not big for a bicycle, it is around 1 second and also the speed is not an impediment to say that the whole prototype fulfills the expectations and objectives of the thesis.

### 6.2 Application of learning

During this thesis I applied all the knowledge gained during the degree on circuits, which was really useful for the simulation and preparation of the circuit for the prototype. Also it was really useful the knowledge on electromagnetic fields to know how this voltage is created by the coil and magnet and how the specification of the coil and more could change the results on the circuit.

1. Análisis y diseño de circuitos
2. Componentes eléctricos y medidas
3. Electronica analógica

## 4. Campos electromagnéticos

### 6.3 Lessons Learned

The most important lesson was to discover what is Energy harvesting, because I had never heard about it before. In my opinion it is a very interesting topic and really useful, that can create such a good things not to waste so much energy.

Also, it was quite new for me all this kind of software related with simulation and I found them very helpful for the realization of my thesis, because they helped me to understand how they worked the circuits and to choose the best option for the final prototype. This choice it was one of the most important part because if i had chosen the wrong IC the whole prototype maybe wouldn't have worked at all.

1. Energy harvesting
2. Circuit design software

### 6.4 Future works

The two main idea that I have right now after all this thesis are:
First, to attach a real USB port to the circuit and try charging a mobile phone.
Second, put all the prototype and circuit in a real bicycle to test it in a real life mode. Also its possible that there are some kind of different components, even values that can dwarf the whole circuit and can be more suitable for a day to day in a bicycle.

### 6.5 Personal Ratings

In my opinion I can assure that this thesis has opened my eyes as to renewable energy and green energy. For sure I will continue research in this area, because I find it very attractive for a better future and there are a lot of possibilities with different things not only electromagnetic.

## Appendix A

## Theoretical Calculation

## A. 1 Magnetic flux Generated by the Bar Magnet

The bar magnet is modeled as two point magnetic charges situated at $l_{m} / 2$ on the y axis. The magnitude of the magnetic point charges, $q_{m}$, is obtained by integrating the magnetization, $\mu M$, over the cross-sectional areas of the magnet ends. Thus,

$$
\begin{equation*}
q_{m}=\mu_{o} M \pi r_{m}^{2} \tag{A.1}
\end{equation*}
$$



Figure A.1: Magnetic flux density from a bar magnet.

The magnetic flux density at a given point, B , depends on two terms: the magnetic field strength $H_{m}$; and the local magnetization. The local magnetization is M inside the
magnet and 0 outside. Figure A. 1 shows how the contributions from these two terms add up to the magnetic flux density:

$$
\begin{equation*}
B=\mu_{0}\left(H_{m}+M\right) \tag{A.2}
\end{equation*}
$$

As shown in Figure A.1, a bar magnet has a uniform magnetic charge density on its ends at $x=+-l_{m} / 2$. I make the simplifying assumption that the bar magnet can be modeled as two point magnetic charges located on the y -axis at $x=+-l_{m} / 2$. Thus, while the $\mu M$ term I calculate is exact, the $\mu H$ term is an approximation because it comes from a point- charge assumption. I will concentrate on the calculation of $\mu_{0} H_{m}$ and then add it to the simple $\mu_{0} M$ term towards the end to arrive at B inside the magnet. Outside the magnet the $B=\mu_{0} H$ alone.

The total flux emanating from the magnetic charge is $q_{m}$. The resultant flux through any given turn of wire is the fraction of the total flux that passes through the area enclosed by the wire turn; and this flux is numerically equal to the same fraction of $q_{n}$. If a sphere is imagined around the point charge, and a single wire turn intersects the sphere to delineate a spherical cap (Figure A.2),


Figure A.2: Point charge and single wire turn geometry
then it follows from Gauss' Law that the magnetic flux through the wire turn is equal to the magnetic flux escaping through the cap. Thus, the magnetic flux through the wire
turn is proportional to the ratio of the surface area of the cap to the surface area of the entire sphere. For a sphere of radius R, with a distance H from its center to the plane of the coil, the surface area of the cap formed is

$$
\begin{equation*}
A_{c a p}=2 \pi R(R-H) \tag{A.3}
\end{equation*}
$$

Therefore, the magnetic flux through a single wire turn of radius $r_{c}$ at a height H above a point charge $q_{m}$ is given by

$$
\begin{equation*}
\phi=q_{m} 2 \pi R(R-H) / 4 \pi R^{2} \tag{A.4}
\end{equation*}
$$

The magnetic flux through a wire turn in the induction system depends on contributions from the magnetic charges at both ends of the bar magnet. The labeled geometry of the magnetic charges and a single wire turn is shown in Figure A.3. The magnetic charges have opposite signs to represent the North and South poles of the magnet, with $q_{1}$ positive and $q_{2}$ negative. In addition, the direction of the magnetic flux through the wire turn changes when a magnetic charge passes from one side of the wire turn to the other. Sign functions are added to Equation A. 4 to account for these changes in the magnetic flux directions. The magnetic flux contributions and from the magnetic charges $\phi_{1}$ and $\phi_{2}$ respectively are

$$
\begin{align*}
& \phi_{1}=\operatorname{sign}\left(h-\frac{l_{m}}{2}\right) \frac{-q_{m}\left(\sqrt{r_{c}^{2}+\left(h-\frac{l_{m}}{2}\right)^{2}}-\left|h-\frac{l_{m}}{2}\right|\right)}{2 \sqrt{r_{c}^{2}+\left(h-\frac{l_{m}}{2}\right)^{2}}}  \tag{A.5}\\
& \phi_{2}=\operatorname{sign}\left(h+\frac{l_{m}}{2}\right) \frac{q_{m}\left(\sqrt{r_{c}^{2}+\left(h+\frac{l_{m}}{2}\right)^{2}}-\left|h+\frac{l_{m}}{2}\right|\right)}{2 \sqrt{r_{c}^{2}+\left(h+\frac{l_{m}}{2}\right)^{2}}} \tag{A.6}
\end{align*}
$$

$\phi_{1}$ and $\phi_{2}$ are the fluxes from the point charges at the ends of the bar magnet; when they are divided by the area of the wire turn, they sum up to the $\mu_{0} H_{m}$ component of B. In addition, there is magnetic flux inside the bar magnet due to its magnetization; the magnitude of this flux is $\mu_{0} M \pi r_{m}^{2}$, which from Equation A. 1 is equal to $q_{m}$. Therefore the


Figure A.3: Magnetic dipole and single wire turn geometry.
flux due to $\mu_{0}$; term can be expressed as:

$$
\phi_{M}=\left\{\begin{array}{ccc}
q_{m} & \text { si } & -l_{m} / 2<y<l_{m} / 2  \tag{A.7}\\
0 & \text { si } & y<-l_{m} / 2 U l_{m} / 2<y
\end{array}\right.
$$

The total magnetic flux through a single wire turn at height $h$ is the sum of $\phi_{1}, \phi_{2}$ and $\phi_{M}$ from Equation A. 5 , A. 6 and A. 7 respectively. This sum is multiplied by the number of turns of wire per unit height, $N / l_{c}$, and a small incremental height, $d y$, to obtain the magnetic flux through all the wires coiled at height $h$. The total magnetic flux through the coil of length $l_{c}$ is the integral of the magnetic flux over the height of the coil:

$$
\begin{equation*}
\phi_{\text {Total }}=\int_{h}^{h+l_{c}} \frac{N\left(\phi_{1}+\phi_{2}+\phi_{M}\right)}{l_{c}} d_{y} \tag{A.8}
\end{equation*}
$$

## A.1.1 Coil Inductance and Resistance

The inductance of the coil, $L_{C}$, is a function of the number of turns, cross-sectional area, and height of the coil. The inductance for a long thin coil, where $l_{c}>\sqrt{A_{c}}$, is given by:

$$
\begin{equation*}
L_{c}=\frac{\mu_{0} N^{2} A_{c}}{l_{c}}=\frac{\mu_{0} \pi N^{2} r_{c}^{2}}{l_{c}} \tag{A.9}
\end{equation*}
$$

The resistance of the coil, $R_{c}$, depends on the resistivity of the wire material, $\rho$, the length of the coiled wire, $I_{w}$, and the cross-sectional area of the wire, $A_{w}$, If the radius of the wire is $r_{w}$, I have

$$
\begin{gather*}
l_{w}=N \pi d_{c}  \tag{A.10}\\
A_{w}=\pi r_{w}^{2}  \tag{A.11}\\
R_{c}=\frac{\rho l_{w}}{A_{w}}=\frac{\rho\left(N 2 \pi r_{c}\right.}{\pi r_{c}^{2}}=\frac{2 N \rho r_{c}}{r_{w}^{2}} \tag{A.12}
\end{gather*}
$$

If $R_{c} \gg 2 \pi f L_{C}$, the effects of the system inductance are negligible in comparison to those of the system resistance. Since this relation often holds true in real systems, the subsequent analysis assumes that the resistance effects dominate the system

## A. 2 Voltage and Power Generation

Faraday's Law states that the open-circuit voltage induced across a turn of wire is the negative integral of the time-change in magnetic flux over the cross-sectional area of the turn. By the chain rule of differentiation, the time-change in magnetic flux can be separated into two multiplicative terms - the change in magnetic flux over height, and the change in coil height over time (in other words, the velocity of the coil). Thus,

$$
\begin{equation*}
V=\int \frac{\left.d \phi_{t} o t a l\right)}{d t} d_{A}=\int \frac{\left.d \phi_{t} o t a l\right)}{d h} \frac{d h)}{d t} d_{A} \tag{A.13}
\end{equation*}
$$

The formula for $\frac{\left.d \phi_{t} o t a l\right)}{d h}$ can be calculated by differentiating Equation A. 8 to arrive at

$$
\begin{equation*}
\frac{d \phi_{t} o t a l}{d h}=\frac{d}{d h} \int_{h}^{h+l_{c}} \frac{N\left(\phi_{1}+\phi_{2}\right)}{l_{c}} d_{h} \tag{A.14}
\end{equation*}
$$

Given the velocity of the coil, $v$, the open-circuit voltage induced across the coil can be calculated:

$$
\begin{equation*}
V=\int_{h}^{h+l_{c}} \frac{v N\left(\phi_{1}+\phi_{2}\right)}{l_{c}} d_{A} \tag{A.15}
\end{equation*}
$$

$P$ is the power delivered by the system to a load, modeled here as a resistor $R_{I}$. Since the system inductance is assumed to be negligible, the open-circuit voltage generated across the ends of the coil is now applied across the resistances $R_{c}$, and $R_{L}$ in series. Then, Kirchhoff's Voltage Law implies that

$$
\begin{equation*}
V=V_{c}+V_{L} \tag{A.16}
\end{equation*}
$$

where $V_{c}$, and $V_{L}$ are the voltages across the coil and load resistor respectively. $I$ is the resultant current flowing through the circuit. Ohm's Law states that the voltage across a resistor is the product of the resistance and the current flowing through it; applying this to Equation A. 16 allows us to solve for the value of $I$ :

$$
\begin{gather*}
V=I\left(R_{C}+R_{L}\right)  \tag{A.17}\\
I=\frac{V}{\left(R_{C}+R_{L}\right)} \tag{A.18}
\end{gather*}
$$

The instantaneous power dissipated across the load resistance is the product of the current flowing through it and the voltage across it. This gives

$$
\begin{equation*}
P=V_{l} I=\left(R_{l} I^{2}\right) \tag{A.19}
\end{equation*}
$$

and substituting the value for $I$ from Equation A.18,

$$
\begin{equation*}
P=\frac{R_{L} V^{2}}{\left(R_{C}+R_{L}\right)^{2}} \tag{A.20}
\end{equation*}
$$

Since $R_{L}$ is fixed, I differentiate $P$ with respect to $R_{L}$ to find the maximum:

$$
\begin{equation*}
\frac{d P}{d R_{l}}=\frac{V^{2}}{\left(R_{c}+R_{l}\right)^{2}}-\frac{2 R_{l} V^{2}}{\left(R_{c}+R_{l}\right)^{3}}=0 ;\left(R_{c}+R_{l}\right)-2 R_{l}=0 ; R_{l}=R_{c} \tag{A.21}
\end{equation*}
$$

Hence, the load resistance should be matched to the coil resistance in order to extract the maximum possible power from the system.

## A.2.1 Magnetic Field Generated by the Magnets

Within the system with magnets, there are two regions: Region A, between $x=0$ and $x=X_{A}$, with the magnets; and Region B , between $x=0$ and $x=-X_{B}$, with the air
gap and coils. These regions have distinct magnetic fields, $H_{A}$ and $H_{B}$ respectively. The interface between the magnetic region and the air gap provides the boundary conditions on the fields in these two regions. The x -axis is defined such that $x=0$ at the interface between the magnets and air. The magnetic charge is concentrated on the planes at the ends of the magnets at $x=0$. The magnetic charge density on the z -axis is represented by $\phi_{M}(z)$. Figure A. 4 shows a schematic of the magnet placement and the resulting graph of $\phi_{M}(z)$ as a function of z . The charge density function from Figure A. 4 can be represented by a Fourier series. Then I can solve for the magnetic field caused by a sine wave charge distribution, and use superposition to get the total field.

The charge density waveform can be represented by

$$
\begin{equation*}
\sigma_{M}=a_{0\left(\phi_{M}\right.}+\sum_{k=1}^{\infty}\left(a_{k(\phi M)} \cos \left(\frac{2 \pi k z}{Z}\right)+b_{k(\phi M)} \sin \left(\frac{2 \pi k z}{Z}\right)\right) \tag{A.22}
\end{equation*}
$$

where Z is the spatial period of the magnetic charge density function and the Fourier coefficients are:

$$
\begin{equation*}
a_{0\left(\sigma_{M}\right)}=0 \tag{A.23}
\end{equation*}
$$

$$
\begin{equation*}
a_{k\left(\sigma_{M}\right)}=0 \tag{A.24}
\end{equation*}
$$

$$
b_{k\left(\sigma_{M}\right)}=\left\{\begin{array}{lll}
\frac{4 \mid s i g m a_{\max }}{k \pi} \cos \frac{\pi k d}{l+2 d} & \text { si } & \text { for odd } \mathrm{k}  \tag{A.25}\\
0 & \text { si } & \text { for even } \mathrm{k}
\end{array}\right.
$$



Figure A.4: Schematic of the magnet placement and the resulting charge density on the z-axis.

Since the magnetic charge density waveform is reducible to a sum of sines, I solve for the magnetic fields resulting from a sinusoidal charge density $\left(\sigma_{M k}=b_{k\left(\sigma_{M}\right)} \sin \left(\frac{2 \pi k z}{Z}\right)\right)$ on the z-axis. For a system with current $J$, Maxwell's Equations state that:

$$
\begin{equation*}
\nabla \times H=J \tag{A.26}
\end{equation*}
$$

$$
\begin{equation*}
\nabla * B=0 \tag{A.27}
\end{equation*}
$$

Since I are solving the part of the superposition that only considers the fields due to the magnets, there is no current in the system and $J$ in Equation A. 26 is zero. This means that the curl of $H$ is zero, which implies that $H$ is the negative gradient of some scalar magnetic potential function $\psi$.

$$
\begin{gather*}
\nabla \times H=0  \tag{A.28}\\
\Rightarrow H=-\nabla_{\psi} \tag{A.29}
\end{gather*}
$$

From Equations A.2, A.27, A. 28 and A. 29 I get

$$
\begin{equation*}
\nabla * \mu(-a \nabla \psi+M)=0 \tag{A.30}
\end{equation*}
$$

Because the magnetization $M$ of a magnet is a constant, and $M$ of air is zero, in both cases $\nabla * M$ vanishes. Thus I get the simplified equation

$$
\begin{equation*}
\nabla^{2} \psi=0 \tag{A.31}
\end{equation*}
$$

This equation must be solved for regions $A$ and $B$ to obtain the corresponding magnetic potentials ( $\psi A$ and $\psi B$ ) in those regions. To satisfy Equation A.31, the solutions must be of the form $\psi_{A}=\left[\alpha_{1} \sin \frac{2 \pi k z}{Z}+\alpha_{2} \cos \frac{2 \pi k z}{Z}\right] x\left[\alpha_{3} \sinh \frac{2 \pi k z}{Z}+\alpha_{4} \cosh \frac{2 \pi k z}{Z}\right] \psi_{B}=\left[\beta_{1} \sin \frac{2 \pi k z}{Z}+\right.$ $\left.\beta_{2} \cos \frac{2 \pi k z}{Z}\right] x\left[\beta_{3} \sinh \frac{2 \pi k z}{Z}+\beta_{4} \cosh \frac{2 \pi k z}{Z}\right]$

The values of the constants in these equations are obtained by applying the boundary conditions on the regions. The first two boundary conditions arise at the interfaces with the magnetically permeable backings at $x=x_{A}$ and $x=-x_{B}$. Given the absence of surface currents at these interfaces, the tangential magnetic field, $H_{z}$ is conserved.

I have assumed that the materials have $\mu=\infty$; therefore $B=\mu H$ dictates that $H=0$ in order for $B$ to be finite. Since $H=0$, the tangential field $H_{z}$ must be zero at these interfaces. The interface between the magnets and air at $x=0$ is considered next. The conservation of the tangential magnetic field, $H z$, (given the absence of surface currents at $\mathrm{x}=0$ ), and the conservation of the normal magnetic flux, $B_{x}$, yield two more boundary conditions for the system. In conclusion, the boundary conditions applicable are :

1. $H_{A_{z}}=0$ at $x=x_{A}$
2. $H_{B_{Z}}=0$ at $x=-x_{B}$.
3. $H_{A_{z}}=H_{B_{z}}$ at $x=0$
4. $\mu_{0} H_{A_{z}}=H_{B_{z}}$ at $x=0$

Solving for the values of the constants is now a matter of algebraic manipulation. Boundary conditions (1) and (2) state that $H_{A_{z}}$ and $H_{B_{z}}$, are zero-valued at $x_{A}$ and $-x_{B}$ respectively. $H_{A_{z}}$ and $H_{B_{z}}$, are the partial derivatives of $-\psi_{A}$ and $\psi_{B}$ with respect to $z$, so for them to be zero at $x_{A}$ and $-x_{B}$ respectively, the x-dependent components of $-\psi_{A}$ and $\psi_{B}$ must be zero.

This means that the x -dependent components of the magnetic potentials must be sinh functions, since cosh functions cannot be zero-valued at any points. This means that the constants $\alpha_{2}, \alpha_{4}, \beta_{2}$ and $\beta_{4}$ are zero. Constants $\alpha_{1}$ and $\alpha_{3}$ can be combined into $\alpha$, and
$\beta_{1}$ and $\beta_{3}$ into $\beta$.

$$
\begin{align*}
& \psi_{A}=\alpha \sin \left(\frac{2 \pi k z}{Z}\right) \sinh \left(\frac{2 \pi\left(x-x_{A}\right)}{Z}\right)  \tag{A.32}\\
& \psi_{B}=\beta \sin \left(\frac{2 \pi k z}{Z}\right) \sinh \left(\frac{2 \pi\left(x+x_{B}\right)}{Z}\right) \tag{A.33}
\end{align*}
$$

Now I have two equations (boundary conditions (3) and (4)) and two unknowns (the values of the two constants $\alpha$ and $\beta$ ); the following steps show the rearrangement of variables to arrive at the answer.

$$
\begin{align*}
& \alpha=\frac{b_{k\left(\alpha_{M}\right)} \sinh \left(\frac{2 \pi k z x_{B}}{Z}\right)}{\frac{2 \pi k z \mu_{0}}{Z}\left(\sinh \left(\frac{2 \pi k z x_{A}}{Z}\right) \cosh \left(\frac{2 \pi k z x_{B}}{Z}\right)+\sinh \left(\frac{2 \pi k z x_{B}}{Z}\right) \cosh \left(\frac{2 \pi k z x_{A}}{Z}\right)\right)}  \tag{A.34}\\
& \beta=\frac{-b_{k\left(\alpha_{M}\right)} \sinh \left(\frac{2 \pi k z x_{A}}{Z}\right)}{\frac{2 \pi k z \mu_{0}}{Z}\left(\sinh \left(\frac{2 \pi k z x_{A}}{Z}\right) \cosh \left(\frac{2 \pi k z x_{B}}{Z}\right)+\sinh \left(\frac{2 \pi k z x_{B}}{Z}\right) \cosh \left(\frac{2 \pi k z x_{A}}{Z}\right)\right)} \tag{A.35}
\end{align*}
$$



Figure A.5: Schematic of the coil placement and the tangential magnetic field at $-x_{B}$ resulting from current $i$ flowing through all three phases of coils.

From equations A.22, A. 32 and A.33, the total magnetic potential due to the magnets
is :

$$
\begin{align*}
& \psi_{A_{(\text {magnets })}}=\sum_{k=1}^{\infty} \alpha \sinh \left(\frac{2 \pi k\left(x-x_{A}\right)}{2(l+2 d)}\right) \sin \left(\frac{2 \pi k z}{2(l+2 d)}\right)  \tag{A.36}\\
& \psi_{B_{(\text {magnets })}}=\sum_{k=1}^{\infty} \beta \sinh \left(\frac{2 \pi k\left(x+x_{B}\right)}{2(l+2 d)}\right) \sin \left(\frac{2 \pi k z}{2(l+2 d)}\right) \tag{A.37}
\end{align*}
$$

## A.2.2 Magnetic Field Generated by Coil Current

For the calculation of the fields due to current flowing through the coils, the magnets are ignored. The current through the coils is approximated as a surface current at $x=-x_{B}$. This means that there is no difference between Region A and Region B for this calculation. Thus I solve for the magnetic fields from the coils in the region bounded by $x_{A}$ and $-x_{B}$. Figure A. 5 shows a graph of the tangential magnetic field $H_{z}$, at $-x_{B}$ that would result from a current $i$ flowing through all three phases of coils.

The tangential magnetic field at the surface of the magnetic backing is the sum of the contributions from the three phases A, B and C. The width of each phase is $2 g$, and the gap between phases is $t$. Since the three phases are symmetric, I can solve for one phase and then use superposition to add in the effects from the other two phases. In particular, I will solve for the contribution from current i flowing through the phase A coils. The tangential magnetic field, $H_{z}$, at plane $x=-x_{B}$, due to the current $i$ passing through the phase A coils, can be expressed as

$$
\begin{equation*}
H_{z}=a_{0\left(H_{z}\right)}+\sum_{k=1}^{\infty}\left[a_{k\left(H_{z}\right)} \cos \left(\frac{2 \pi k z}{Z}\right)+b_{k\left(H_{z}\right)} \sin \left(\frac{2 \pi k z}{Z}\right)\right] \tag{A.38}
\end{equation*}
$$

where $Z$, the spatial period of the tangential magnetic field function, is $6(2 g+t)$, and the Fourier coefficients are

$$
\begin{equation*}
a_{0\left(H_{z}\right)}=0 \tag{A.39}
\end{equation*}
$$

$$
a_{k\left(H_{z}\right)}= \begin{cases}\frac{4 i}{g k \pi} \sin \left(\frac{\pi k g}{3(2 t+g)}\right) & \text { for odd } \mathrm{k}  \tag{A.40}\\ 0 & \text { for even } \mathrm{k}\end{cases}
$$

$$
\begin{equation*}
b_{k\left(H_{z}\right)}=0 \tag{A.41}
\end{equation*}
$$

Since $H z$ can be expressed as a sum of cosines, I can solve for the contribution from a single harmonic ( $H_{z k}=a_{k(H z)} \cos \left(\frac{2 \pi k z}{Z}\right)$ and then use superposition to obtain the complete solution. Similarly to the case of the magnets, the boundary conditions on the magnetic field due to coil current are:

1. $H_{z}=0$ at $x=x_{A}$
2. $H_{z}=a_{k(H z)} \cos \left(\frac{2 \pi k z}{Z}\right)$ at $x=-x_{B}$.

Within the region, similar to the case with the magnets,

$$
\nabla \times H=0 \Rightarrow H=-\nabla \psi \Rightarrow \nabla^{2} \psi=0
$$

The solution of this equation is the magnetic potential (0) due to the current in the coils, and must be of the form

$$
\psi=\left[D_{1} \sin \left(\frac{}{2 \pi k z} Z\right)+D_{2} \cos \left(\frac{}{2 \pi k z} Z\right)\right] \times\left[D_{3} \sinh \left(\frac{}{2 \pi k x} Z\right)+D_{4} \cosh \left(\frac{}{2 \pi k x} Z\right)\right] .
$$

Since boundary condition (1) states that $H_{z}$, must be zero at $x_{A}$, the x-dependent component of the magnetic potential must be a sinh function.

$$
\begin{aligned}
& \psi=D \sin \left(\frac{2 \pi k z}{Z}\right) \sinh \left(\frac{2 \pi k\left(x-x_{A}\right)}{Z}\right) \\
& \left.\Rightarrow H_{z}\right|_{x=x_{A}}=-\left.\frac{2 \pi k D}{Z} \cos \left(\frac{2 \pi k z}{Z}\right) \sinh \left(\frac{2 \pi k\left(x-x_{A}\right)}{Z}\right)\right|_{x=x_{A}}=0
\end{aligned}
$$



Figure A.6: Three-phase coil arrangement geometry.

From boundary condition (2), $H_{z}$ is $a_{k\left(H_{z}\right)} \cos \left(\frac{2 \pi k z}{Z}\right)$ at $-x_{B}$.

$$
\begin{array}{r}
\left.H_{z}\right|_{x=-x_{B}}=-\left.\frac{2 \pi k D}{Z} \cos \left(\frac{2 \pi k z}{Z}\right) \sinh \left(\frac{2 \pi k\left(x-x_{A}\right)}{Z}\right)\right|_{x=x_{A}}=a_{k\left(H_{z}\right)} \cos \left(\frac{2 \pi k z}{Z}\right) \\
D=\frac{a_{k\left(H_{z}\right)} Z}{2 \pi k \sinh \left(\frac{2 k k\left(x_{A}+x_{B}\right)}{Z}\right)} \\
\psi_{\text {coils }}=\sum_{k=1}^{\infty} D \sinh \left(\frac{2 \pi k\left(x-x_{A}\right)}{6(2 g+t)}\right) \sin \left(\frac{2 \pi k z}{6(2 g+t)}\right) \tag{А.43}
\end{array}
$$

## A.2.3 Coil Self-Inductance, Mutual Inductance, and Resistance

Equation A. 43 allows us to calculate the magnetic potential created by the flow of current through the coils; the magnetic flux density generated can be obtained from this magnetic potential.

$$
B_{c o i l s}=\mu_{0} H_{c o i l s}=-\mu_{0} \nabla \psi_{\text {coils }}
$$

The magnetic fluxes through the coils due to current through them are $\lambda_{c(A)}, \lambda_{c(B)}$ and $\lambda_{c(C)}$ through phase A, B and C respectively, and can be calculated by multiplying the magnetic flux density and the area of the coils. Figure A. 6 shows the geometry of the three phases. For example, the magnetic flux through phase A coils is:

$$
\lambda_{c(A)}=B_{\text {coils }} \cdot A_{A}
$$

where $A_{A}$ is the area of the phase A coils. Since the coils lie in the $x=-x_{B}$ plane, only he x-component of the magnetic flux density will pass through them; hence $B_{\text {coils }} \Delta A_{A}=$ $B_{x(\text { coils })} A_{A}$.

The self-inductance, $L$, of a coil is defined as the magnetic flux generated through the coil due to the flow of a unit current through it. The mutual inductance between a pair of coils, $M$, is defined as the magnetic flux generated through one coil due to the flow of a unit current through the other. The magnetic flux through each phase is influenced by the current flowing through every phase. Since everything is symmetric across phases, the self-inductance of each phase and the mutual inductance between each pair of phases is the same. Equation defines the dependence of the magnetic fluxes and the current through the coils.

$$
\left[\begin{array}{l}
\lambda_{c(A)}  \tag{A.44}\\
\lambda_{c(B)} \\
\lambda_{c(C)}
\end{array}\right]=\left[\begin{array}{ccc}
L & -M & -M \\
-M & L & -M \\
-M & -M & L
\end{array}\right]\left[\begin{array}{l}
i_{A} \\
i_{B} \\
i_{C}
\end{array}\right]
$$

To calculate the value of $L$ and $M$, I consider the flux linked by a phase A coil and a phase B coil due to a current $i$ flowing through the phase A coil (when $i_{B}$ and $i_{C}$ are 0 ):

$$
\begin{aligned}
& \lambda_{c(A)}=B_{x(\text { coils })} A_{A}=n N \int \frac{-l}{2} \frac{l}{2} \mu_{0} H_{x(c o i l s)} w d z=L i \\
& \lambda_{c(B)}=B_{x(\text { coils })} A_{B}=n N \int \frac{2 g+t-l}{2} \frac{2 g+t+l}{2} \mu_{0} H_{x(c o i l s)} w d z=L i
\end{aligned}
$$

The integrals are the flux through one coil and one turn of wire; to get the total flux they are multiplied by the number of coils (which should be the same as the number of magnetic poles, $n$ ), and the number of turns of wire ( N ) in each coil. The turns of wire in the coil are approximated into a point-wise lumped distribution; therefore I just multiply by the number of wire turns instead of integrating over the physical width of the turns ( $2 g$ for each phase). Rearranging the terms, I get:

$$
\begin{align*}
& L=\frac{n N}{i} \int \frac{-l}{2} \frac{l}{2} \mu_{0} H_{x(\text { coils })} w d z  \tag{A.45}\\
& M=\frac{n N}{i} \int \frac{-l}{2} \frac{l}{2} \mu_{0} H_{x(\text { cooils) })} w d z . \tag{A.46}
\end{align*}
$$

Since $H_{x(\text { coils })}$ as $a$ function of $i$ can be calculated from Equation A-43, the values of $L$ and $M$ can be found.

The resistance of all the coil phases should be the same since they are the same pattern displaced in space. The resistance of each phase depends on the resistivity of the wire material, $\rho W$, the cross-sectional area of the wire, $A_{W}$, and the total length of the wire, $l_{w}$. The length of wire used will depend on the number of turns of wire and on the pattern of winding.

$$
\begin{equation*}
R=\frac{\rho_{w} l_{w}}{A_{w}} \tag{A.47}
\end{equation*}
$$

## A.2.4 Voltage and Power Generation

The magnetic fields in the system are linear; therefore superposition can be used and the total magnetic field is the sum of the magnetic fields from the magnets and the coils.

$$
H_{\text {total }}=\left\{\begin{array}{ll}
-\nabla\left(\psi_{A(\text { magnets })}+\psi_{\text {coils }}\right) & 0 \leqslant x \leqslant x_{A}  \tag{A.48}\\
-\nabla\left(\psi_{B(\text { coils })}+\psi_{\text {magnets }}\right) & 0 \geqslant x \geqslant-x_{B}
\end{array} \quad B_{\text {total }}=\mu H_{\text {total }} .\right.
$$

The magnetic fluxes through the coils due to the magnets, $\left.\lambda_{m(A)}, \lambda_{m(B)}\right)$ and $\lambda_{m(C)}$ through phases A, B and C respectively, are calculated by multiplying the magnetic flux
density and the area of the coils.

$$
\left[\begin{array}{l}
\lambda_{m(A)}  \tag{A.49}\\
\lambda_{m(B)} \\
\lambda_{m(C)}
\end{array}\right]=\left[\begin{array}{l}
B_{x(\text { magnets })} A_{A} \\
B_{x(\text { magnets })} A_{B} \\
B_{x(\text { magnets })} A_{C}
\end{array}\right]
$$

By superposition, the total magnetic flux through the coils is the sum of the fluxes generated by the magnets and by the flow of current through the coils.

$$
\left[\begin{array}{l}
\lambda_{A}  \tag{A.50}\\
\lambda_{B} \\
\lambda_{C}
\end{array}\right]=\left[\begin{array}{l}
\lambda_{c(A)} \\
\lambda_{c(B)} \\
\lambda_{c(C)}
\end{array}\right]+\left[\begin{array}{l}
\lambda_{m(A)} \\
\lambda_{m(B)} \\
\lambda_{m(C)}
\end{array}\right]=\left[\begin{array}{ccc}
L & -M & -M \\
-M & L & -M \\
-M & -M & L
\end{array}\right]\left[\begin{array}{l}
i_{A} \\
i_{B} \\
i_{C}
\end{array}\right]+\left[\begin{array}{l}
B_{x(\text { magnets })} A_{A} \\
B_{x(\text { magnets })} A_{B} \\
B_{x(\text { magnets })} A_{C}
\end{array}\right]
$$

In order for these equations to hold true, it is important that the magnetic backing of the coils does not saturate due to the magnetic flux through it. Figure A. 7 shows the path of the flux through the magnetically permeable backings. $B \cdot A$ should be calculated for the area under half a magnet, and should be equated to $B_{\text {new }} \cdot A_{\text {new }}$, where $A_{\text {new }}$ is the cross-sectional area of the magnetic backing through which the flux will pass. A $B H$ chart of the backing material should be consulted to confirm that $B_{\text {new }}$ will not cause it to saturate. A similar check should be conducted for the backing of the magnets.


Figure A.7: Path of the magnetic flux in a magnet-across-coils system.

Faraday's law is invoked again in order to calculate the voltage generated across the coils. $\lambda_{A}, \lambda_{B}$ and $\lambda_{C}$ are known as a function of position, so $\frac{d \lambda}{d z}$ can be calculated for each phase. These values, when multiplied by the velocity of the coil $\left(\frac{d z}{d t}\right)$, give $\frac{d \lambda}{d t}$ for each respective phrase. Since the phases are identical except for a displacement in space, the voltage through them will be identical except displaced in time.

$$
\frac{d}{d t}\left[\begin{array}{l}
\lambda_{A}  \tag{A.51}\\
\lambda_{B} \\
\lambda_{C}
\end{array}\right]=\left[\begin{array}{l}
V_{A} \\
V_{B} \\
V_{C}
\end{array}\right]-\left[\begin{array}{lll}
R & 0 & 0 \\
0 & R & 0 \\
0 & 0 & R
\end{array}\right]\left[\begin{array}{c}
i_{A} \\
i_{B} \\
i_{C}
\end{array}\right]
$$

Equations A. 50 and A. 51 give us a system of 9 equations and 9 variables: the variables are the magnetic fluxes, currents, and voltages for the three phases; the resistance, selfinductance, and mutual inductance of the coils are known.

Now that I can solve for the output voltage of the system, I consider the dissipation of the power produced. Applying Ohm's law to the system connected to a load resistor $R_{L}$ gives:

$$
\left[\begin{array}{c}
V_{A}  \tag{A.52}\\
V_{B} \\
V_{C}
\end{array}\right]=-\left[\begin{array}{ccc}
R_{L} & 0 & 0 \\
0 & R_{L} & 0 \\
0 & 0 & R_{L}
\end{array}\right]\left[\begin{array}{c}
i_{A} \\
i_{B} \\
i_{C}
\end{array}\right]
$$

If $R \gg \omega L$, where w is the operating frequency of the system in $\mathrm{rad} / \mathrm{s}$, the effect of inductances $L$ and $M$ is negligible compared to that of the resistance $R$. In conclusion $R_{L}$ should be equal to $R$ in order to extract the maximum possible power from the system, the instantaneous power dissipated through $R_{L}$ being:

$$
\left[\begin{array}{c}
P_{A}  \tag{A.53}\\
P_{B} \\
P_{C}
\end{array}\right]=\frac{R_{L}}{\left(R+R_{L}\right)^{2}}\left[\begin{array}{c}
V_{A}^{2} \\
V_{B}^{2} \\
V_{C}^{2}
\end{array}\right]
$$

Appendix B

Datasheet LTC3108

## features

- Operates from Inputs of 20 mV
- Complete Energy Harvesting Power Management System
- Selectable $\mathrm{V}_{\text {OUt }}$ of $2.35 \mathrm{~V}, 3.3 \mathrm{~V}, 4.1 \mathrm{~V}$ or 5 V
- LDO: 2.2 V at 3 mA
- Logic Controlled Output
- Reserve Energy Output
- Power Good Indicator
- Uses Compact Step-Up Transformers
- Small 12-Lead ( $3 \mathrm{~mm} \times 4 \mathrm{~mm}$ ) DFN or 16-Lead SSOP Packages


## APPLICATIONS

- Remote Sensors and Radio Power
- Surplus Heat Energy Harvesting
- HVAC Systems
- Industrial Wireless Sensing
- Automatic Metering
- Building Automation
- Predictive Maintenance


## DESCRIPTION

The LTC ${ }^{\circledast} 108$ is a highly integrated DC/DC converter ideal for harvesting and managing surplus energy from extremely low input voltage sources such as TEGs (thermoelectric generators), thermopiles and small solar cells. The step-up topology operates from input voltages as low as 20 mV . The LTC3108 is functionally equivalent to the LTC3108-1 except for its unique fixed $V_{\text {OUT }}$ options.

Using a small step-up transformer, the LTC3108 provides a complete power management solutionforwireless sensing and data acquisition. The 2.2V LDO powers an external microprocessor, while the main output is programmed to one of four fixed voltages to power a wireless transmitter or sensors. The power good indicator signals that the main output voltage is within regulation. A second output can be enabled by the host. A storage capacitor provides power when the input voltage source is unavailable. Extremely low quiescent current and high efficiency design ensure the fastest possible charge times of the output reservoir capacitor.
The LTC3108 is available in a small, thermally enhanced 12-lead ( $3 \mathrm{~mm} \times 4 \mathrm{~mm}$ ) DFN package and a 16 -lead SSOP package.

## TYPICAL APPLICATION

Wireless Remote Sensor Application Powered From a Peltier Cell

$\mathrm{V}_{\text {OUT }}$ Charge Time


## ABSOLUTE MAXIMUM RATINGS (Note 1)

| SW Voltage .......................................... -.3 V to 2 V |  |
| :---: | :---: |
| C1 Voltage...........................................-0.3V to 6V | VLDO, VSTORE ...................................... -3.3 V to 6V |
| C2 Voltage (Note 5)...................................-8V to 8V | Operating Junction Temperature Range |
| $\mathrm{V}_{\text {OUT2 }}, \mathrm{V}_{\text {OUT2_EN................................... }}$-0.3V to 6V | (Note 2)......................................... $-40^{\circ} \mathrm{C}$ to $125^{\circ} \mathrm{C}$ |
| VAUX...........................................15mA into VAUX | Storage Temperature Range................ $-65^{\circ} \mathrm{C}$ to $125^{\circ} \mathrm{C}$ |

## PIn CONFIGURATION

| TOP VIEW |  |  |
| :---: | :---: | :---: |
|  | GND 1 | 16 GND |
| VAUX -1.1 | VAUX 2 | 15 SW |
|  | VStORE 3 | 14.62 |
| $V_{\text {OUT }}$ (3I: 13 l | VOUT 4 | $13 \mathrm{C1}$ |
|  | $\mathrm{V}_{\text {OUT2 }} 5$ | 12 VOUT2_EN |
| VLDO 5 5! $\quad 180$ VS1 | VLDO 6 | 11 VS1 |
| PGD [6] (__ \% I77 VS2 | PGD 7 | 10 VS2 |
| DE PACKAGE | GND 8 | 9 GND |
| 12-LEAD ( $4 \mathrm{~mm} \times 3 \mathrm{~mm}$ ) PLASTIC DFN | GN PACKAGE 16-LEAD PLASTIC SSOP NARROW$\mathrm{T}_{\mathrm{JMAX}}=125^{\circ} \mathrm{C}, \theta_{\mathrm{JA}}=110^{\circ} \mathrm{C} / \mathrm{W}$ |  |
| $\begin{gathered} \mathrm{T}_{\mathrm{JMAX}}=125^{\circ} \mathrm{C}, \theta_{\mathrm{JA}}=43^{\circ} \mathrm{C} / \mathrm{W} \\ \text { EXPOSED PAD (PIN 13) IS GND, MUST BE SOLDERED TO PCB (NOTE 4) } \end{gathered}$ |  |  |

## ORDER InFORMATION

| LEAD FREE FINISH | TAPE AND REEL | PART MARKING* | PACKAGE DESCRIPTION | TEMPERATURE RANGE |
| :--- | :--- | :--- | :--- | :--- |
| LTC3108EDE\#PBF | LTC3108EDE\#TRPBF | 3108 | 12 -Lead $(4 \mathrm{~mm} \times 3 \mathrm{~mm})$ Plastic DFN | $-40^{\circ} \mathrm{C}$ to $125^{\circ} \mathrm{C}$ |
| LTC3108IDE\#PBF | LTC3108IDE\#TRPBF | 3108 | 12 -Lead $(4 \mathrm{~mm} \times 3 \mathrm{~mm})$ Plastic DFN | $-40^{\circ} \mathrm{C}$ to $125^{\circ} \mathrm{C}$ |
| LTC3108EGN\#PBF | LTC3108EGN\#TRPBF | 3108 | 16 -Lead Plastic SSOP | $-40^{\circ} \mathrm{C}$ to $125^{\circ} \mathrm{C}$ |
| LTC3108IGN\#PBF | LTC3108IGN\#TRPBF | 3108 | 16 -Lead Plastic SSOP | $-40^{\circ} \mathrm{C}$ to $125^{\circ} \mathrm{C}$ |

Consult LTC Marketing for parts specified for other fixed output voltages or wider operating temperature ranges.
*The temperature grade is identified by a label on the shipping container.
For more information on lead free part marking, go to: http://www.linear.com/leadfree/
For more information on tape and reel specifications, go to: http://www.linear.com/tapeandreel/

ELECTRICRL CHARACTERISTICS The • denotes the specifications which apply over the full operating
junction temperature range, otherwise specifications are for $\mathrm{T}_{\mathrm{A}}=25^{\circ} \mathrm{C}$ (Note 2). VAUX $=5 \mathrm{~V}$, unless otherwise noted.

| PARAMETER | CONDITIONS | MIN | TYP | MAX |
| :--- | :--- | :---: | :---: | :---: |
| UNITS |  |  |  |  |
| Minimum Start-Up Voltage | Using 1:100 Transformer Turns Ratio, VAUX = OV | 20 | 50 | mV |
| No-Load Input Current | Using 1:100 Transformer Turns Ratio; $V_{\text {IN }}=20 \mathrm{mV}$, <br> $V_{\text {OUT2_EN }}=$ OV; All Outputs Charged and in Regulation |  | 3 | mA |
| Input Voltage Range | Using 1:100 Transformer Turns Ratio | $\bullet$ | $V_{\text {STARTUP }}$ | 500 |
|  |  | mV |  |  |

ELECTRICAL CHARACTERISTICS The • denotes the specifications which apply over the full operating
junction temperature range, otherwise specifications are for $\mathrm{T}_{A}=25^{\circ} \mathrm{C}$ (Note 2). VAUX $=5 \mathrm{~V}$, unless otherwise noted.

| PARAMETER | CONDITIONS |  | MIN | TYP | MAX | UNITS |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Output Voltage | $\begin{aligned} & \text { VS1 = VS2 = GND } \\ & \text { VS1 = VAUX, VS2 = GND } \\ & \text { VS1 = GND, VS2 = VAUX } \\ & \text { VS1 = VS2 = VAUX } \end{aligned}$ | $\stackrel{\bullet}{\bullet}$ | $\begin{gathered} \hline 2.30 \\ 3.234 \\ 4.018 \\ 4.90 \end{gathered}$ | $\begin{aligned} & \hline 2.350 \\ & 3.300 \\ & 4.100 \\ & 5.000 \end{aligned}$ | $\begin{gathered} \hline 2.40 \\ 3.366 \\ 4.182 \\ 5.10 \end{gathered}$ | V V V V |
| Vout Quiescent Current | $\mathrm{V}_{\text {OUT }}=3.3 \mathrm{~V}, \mathrm{~V}_{\text {OUT2_EN }}=0 \mathrm{~V}$ |  |  | 0.2 |  | $\mu \mathrm{A}$ |
| VAUX Quiescent Current | No Load, All Outputs Charged |  |  | 6 | 9 | $\mu \mathrm{A}$ |
| LDO Output Voltage | 0.5 mA Load | $\bullet$ | 2.134 | 2.2 | 2.266 | V |
| LDO Load Regulation | For 0mA to 2mA Load |  |  | 0.5 | 1 | \% |
| LDO Line Regulation | For VAUX from 2.5 V to 5 V |  |  | 0.05 | 0.2 | \% |
| LDO Dropout Voltage | $\mathrm{l}_{\text {LDO }}=2 \mathrm{~mA}$ | $\bullet$ |  | 100 | 200 | mV |
| LDO Current Limit | $\mathrm{V}_{\text {LDO }}=0 \mathrm{~V}$ | $\bullet$ | 4 | 11 |  | mA |
| $V_{\text {OUT }}$ Current Limit | $\mathrm{V}_{\text {OUT }}=0 \mathrm{~V}$ | $\bullet$ | 2.8 | 4.5 | 7 | mA |
| VSTORE Current Limit | VSTORE = OV | $\bullet$ | 2.8 | 4.5 | 7 | mA |
| VAUX Clamp Voltage | Current into VAUX $=5 \mathrm{~mA}$ | $\bullet$ | 5 | 5.25 | 5.55 | V |
| VSTORE Leakage Current | VSTORE $=5 \mathrm{~V}$ |  |  | 0.1 | 0.3 | $\mu \mathrm{A}$ |
| $\mathrm{V}_{\text {OUT2 }}$ Leakage Current | $\mathrm{V}_{\text {OUT2 }}=$ OV, $\mathrm{V}_{\text {OUT2_EN }}=0 \mathrm{~V}$ |  |  | 0.1 |  | $\mu \mathrm{A}$ |
| VS1, VS2 Threshold Voltage |  | $\bullet$ | 0.4 | 0.85 | 1.2 | V |
| VS1, VS2 Input Current | VS1 $=$ VS2 = 5V |  |  | 0.01 | 0.1 | $\mu \mathrm{A}$ |
| PGOOD Threshold (Rising) | Measured Relative to the V ${ }_{\text {Out }}$ Voltage |  |  | -7.5 |  | \% |
| PGOOD Threshold (Falling) | Measured Relative to the $\mathrm{V}_{\text {Out }}$ Voltage |  |  | -9 |  | \% |
| PGOOD V 0 L | Sink Current $=100 \mu \mathrm{~A}$ |  |  | 0.15 | 0.3 | V |
| PGOOD $\mathrm{V}_{\text {OH }}$ | Source Current = 0 |  | 2.1 | 2.2 | 2.3 | V |
| PGOOD Pull-Up Resistance |  |  |  | 1 |  | $\mathrm{M} \Omega$ |
| V ${ }_{\text {OUT2_EN }}$ Threshold Voltage | Vout2_EN Rising | $\bullet$ | 0.4 | 1 | 1.3 | V |
| Vout2_EN Pull-Down Resistance |  |  |  | 5 |  | $\mathrm{M} \Omega$ |
| Vout2 Turn-On Time |  |  |  | 5 |  | $\mu \mathrm{S}$ |
| $V_{\text {Out2 }}$ Turn-Off Time | (Note 3) |  |  | 0.15 |  | $\mu \mathrm{S}$ |
| $\mathrm{V}_{\text {OUT2 }}$ Current Limit | $\mathrm{V}_{\text {OUT }}=3.3 \mathrm{~V}$ | $\bullet$ | 0.15 | 0.3 | 0.45 | A |
| $\mathrm{V}_{\text {OUT2 }}$ Current Limit Response Time | (Note 3) |  |  | 350 |  | ns |
| $\mathrm{V}_{\text {OUT2 }} \mathrm{P}$-Channel MOSFET On-Resistance | $\mathrm{V}_{\text {OUT }}=3.3 \mathrm{~V}$ (Note 3) |  |  | 1.3 |  | $\Omega$ |
| N-Channel MOSFET On-Resistance | C2 $=5 \mathrm{~V}$ (Note 3) |  |  | 0.5 |  | $\Omega$ |

Note 1: Stresses beyond those listed under Absolute Maximum Ratings may cause permanent damage to the device. Exposure to any Absolute Maximum Rating condition for extended periods may affect device reliability and lifetime.
Note 2: The LTC3108 is tested under pulsed load conditions such that $T_{J} \approx$ $\mathrm{T}_{\mathrm{A}}$. The LTC3108E is guaranteed to meet specifications from $0^{\circ} \mathrm{C}$ to $85^{\circ} \mathrm{C}$ junction temperature. Specifications over the $-40^{\circ} \mathrm{C}$ to $125^{\circ} \mathrm{C}$ operating junction temperature range are assured by design, characterization and correlation with statistical process controls. The LTC3108I is guaranteed over the full $-40^{\circ} \mathrm{C}$ to $125^{\circ} \mathrm{C}$ operating junction temperature range. Note that the maximum ambient temperature is determined by specific operating conditions in conjunction with board layout, the rated thermal package thermal resistance and other environmental factors. The junction
temperature $\left(T_{J}\right)$ is calculated from the ambient temperature $\left(T_{A}\right)$ and power dissipation ( $P_{D}$ ) according to the formula: $T_{J}=T_{A}+\left(P_{D} \bullet \theta_{\mathrm{JA}}{ }^{\circ} C / W\right)$, where $\theta_{\mathrm{JA}}$ is the package thermal impedance.
Note 3: Specification is guaranteed by design and not $100 \%$ tested in production.
Note 4: Failure to solder the exposed backside of the package to the PC board ground plane will result in a thermal resistance much higher than $43^{\circ} \mathrm{C} / \mathrm{W}$.
Note 5: The absolute maximum rating is a DC rating. Under certain conditions in the applications shown, the peak AC voltage on the C 2 pin may exceed $\pm 8 \mathrm{~V}$. This behavior is normal and acceptable because the current into the pin is limited by the impedance of the coupling capacitor.

## TYPICAL PGRFORMANCE CHARACT $\in$ RISTICS $T_{A}=25^{\circ}$, unless otherwise noted.


$I_{\text {vout }}$ and Efficiency vs $V_{I N}$,
1:100 Ratio Transformer



Ivout and Efficiency vs $\mathrm{V}_{\mathrm{IN}}$,
1:20 Ratio Transformer

$I_{\text {Vout }}$ and Efficiency vs $V_{I N}$,
1:50 Ratio Transformer



## TYPICAL PGRFORMANCE CHARACTERISTICS $T_{A}=25^{\circ}$, unless otherwise noted.


$I_{\text {vout }}$ vs dT and TEG Size, 1:100 Ratio



IVout Vs VIN and Source Resistance, 1:100 Ratio


## Resonant Switching Waveforms



LDO Dropout Voltage


TYPICAL PGRFORMANCE CHARACTERISTICS $T_{A}=25^{\circ}$, unless otherwise noted.

## Start-Up Voltage Sequencing




Enable Input and $V_{\text {OUT2 }}$


10 mA LOAD ON $\mathrm{V}_{\text {OUT2 }}$
$\mathrm{C}_{\text {OUT }}=220 \mu \mathrm{~F}$
$V_{0 U T}$ and PGD Response
During a Step Load


LDO Step Load Response



## PIn FUNCTIONS (DFN/SSop)

VAUX (Pin 1/Pin 2): Output of the Internal Rectifier Circuit and $V_{\text {CC }}$ for the IC. Bypass VAUX with at least $1 \mu \mathrm{~F}$ of capacitance. An active shunt regulator clamps VAUX to 5.25 V (typical).

VSTORE (Pin 2/Pin 3): Output for the Storage Capacitor or Battery. A large capacitor may be connected from this pin to GND for powering the system in the event the input voltage is lost. It will be charged up to the maximum VAUX clamp voltage. If not used, this pin should be left open or tied to VAUX.
$V_{\text {OUt }}$ (Pin 3/Pin 4): Main Output of the Converter. The voltage at this pin is regulated to the voltage selected by VS1 and VS2 (see Table 1). Connect this pin to an energy storage capacitor or to a rechargeable battery.
$V_{\text {OUT2 }}$ (Pin 4/Pin 5): Switched Output of the Converter. Connect this pin to a switched load. This output is open until $V_{\text {OUT2_EN }}$ is driven high, then it is connected to $V_{\text {OUT }}$ through a $1.3 \Omega$ P-channel switch. If not used, this pin should be left open or tied to $\mathrm{V}_{\text {OUT }}$. The peak current in this output is limited to 0.3 A typical.
VLDO (Pin 5/Pin 6): Output of the 2.2V LDO. Connect a $2.2 \mu \mathrm{~F}$ or larger ceramic capacitor from this pin to GND. If not used, this pin should be tied to VAUX.

PGD (Pin 6/Pin 7): Power Good Output. When Vout is within $7.5 \%$ of its programmed value, PGD will be pulled up to VLDO through a $1 \mathrm{M} \Omega$ resistor. If $\mathrm{V}_{\text {OUT }}$ drops $9 \%$ below its programmed value PGD will go low. This pin can sink up to $100 \mu \mathrm{~A}$.
VS2 (Pin 7/Pin 10): Vout Select Pin 2. Connect this pin to ground or VAUX to program the output voltage (see Table 1).

VS1 (Pin 8/Pin 11): Vout Select Pin 1. Connect this pin to ground or VAUX to program the output voltage (see Table 1).
$V_{\text {OUT2_EN }}$ (Pin 9/Pin 12): Enable Input for $V_{\text {OUT2. }}$. $V_{\text {OUT2 }}$ will be enabled when this pin is driven high. There is an internal 5 M pull-down resistor on this pin. If not used, this pin can be left open or grounded.
C1 (Pin 10/Pin 13): Input to the Charge Pump and Rectifier Circuit. Connect a capacitor from this pin to the secondary winding of the step-up transformer.
C2 (Pin 11/Pin 14): Input to the N-Channel Gate Drive Circuit. Connect a capacitor from this pin to the secondary winding of the step-up transformer.

SW (Pin 12/Pin 15): Drain of the Internal N-Channel Switch. Connect this pin to the primary winding of the transformer.

GND (Pins 1, 8, 9, 16) SSOP Only: Ground
GND (Exposed Pad Pin 13) DFN Only: Ground. The DFN exposed pad must be soldered to the PCB ground plane. It serves as the ground connection, and as a means of conducting heat away from the die.

Table 1. Regulated Voltage Using Pins VS1 and VS2

| VS2 | VS1 | V $_{\text {OUT }}$ |
| :---: | :---: | :---: |
| GND | GND | 2.35 V |
| GND | VAUX | 3.3 V |
| VAUX | GND | 4.1 V |
| VAUX | VAUX | 5 V |

## LTC3108

## BLOCK DIAGRAM



## OPERFTOी (Refer to the Block Diagram)

The LTC3108 is designed to use a small external step-up transformer to create an ultralow input voltage step-up DC/DC converter and power manager. It is ideally suited for low power wireless sensors and other applications in which surplus energy harvesting is used to generate system power because traditional battery power is inconvenient or impractical.

The LTC3108 is designed to manage the charging and regulation of multiple outputs in a system in which the
average power draw is very low, but there may be periodic pulses of higher load current required. This is typical of wireless sensor applications, where the quiescent power draw is extremely low most of the time, except for transmit bursts when circuitry is powered up to make measurements and transmit data.

The LTC3108 can also be used to trickle charge a standard capacitor, supercapacitor or rechargeable battery, using energy harvested from a Peltier or photovoltaic cell.

## operation

## Oscillator

The LTC3108 utilizes a MOSFET switch to form a resonant step-up oscillator using an external step-up transformer and a small coupling capacitor. This allows it to boost input voltages as low as 20 mV high enough to provide multiple regulated output voltages for powering other circuits. The frequency of oscillation is determined by the inductance of the transformer secondary winding and is typically in the range of 10 kHz to 100 kHz . For input voltages as low as 20 mV , a primary-secondary turns ratio of about 1:100 is recommended. For higher input voltages, this ratio can be lower. See the Applications Information section for more information on selecting the transformer.

## Charge Pump and Rectifier

The AC voltage produced on the secondary winding of the transformer is boosted and rectified using an external charge pump capacitor (from the secondary winding to pin C1) and the rectifiers internal to the LTC3108. The rectifier circuit feeds current into the VAUX pin, providing charge to the external VAUX capacitor and the other outputs.

## VAUX

The active circuits within the LTC3108 are powered from VAUX, which should be bypassed with a $1 \mu \mathrm{~F}$ capacitor. Larger capacitor values are recommended when using turns ratios of 1:50 or 1:20 (refer to the Typical Application examples). Once VAUX exceeds 2.5 V , the main $\mathrm{V}_{\text {OUT }}$ is allowed to start charging.

An internal shunt regulator limits the maximum voltage on VAUX to 5.25 V typical. It shunts to GND any excess current into VAUX when there is no load on the converter or the input source is generating more power than is required by the load.

## Voltage Reference

The LTC3108 includes a precision, micropower reference, for accurate regulated output voltages. This reference becomes active as soon as VAUX exceeds 2 V .

## Synchronous Rectifiers

Once VAUX exceeds 2V, synchronous rectifiers in parallel with each of the internal diodes take over the job of rectifying the input voltage, improving efficiency.

## Low Dropout Linear Regulator (LDO)

The LTC3108 includes a low current LDO to provide a regulated 2.2 V output for powering low power processors or other low power ICs. The LDO is powered by the higher of VAUX or $V_{\text {OUt. }}$. This enables it to become active as soon as VAUX has charged to 2.3 V , while the $\mathrm{V}_{\text {OUT }}$ storage capacitor is still charging. In the event of a step load on the LDO output, current can come from the main $\mathrm{V}_{\text {OUT }}$ capacitor if VAUX drops below $\mathrm{V}_{\text {OUt }}$. The LDO requires a $2.2 \mu \mathrm{~F}$ ceramic capacitor for stability. Larger capacitor values can be used without limitation, but will increase the time it takes for all the outputs to charge up. The LDO output is current limited to 4 mA minimum.

## $V_{\text {OUT }}$

The main output voltage on $\mathrm{V}_{\text {OUT }}$ is charged from the VAUX supply, and is user programmed to one of four regulated voltages using the voltage select pins VS1 and VS2, according to Table 2. Although the logic threshold voltage for VS1 and VS2 is 0.85 V typical, it is recommended that they be tied to ground or VAUX.
Table 2. Regulated Voltage Using Pins VS1 and VS2

| VS2 | VS1 | V $_{\text {OUT }}$ |
| :---: | :---: | :---: |
| GND | GND | 2.35 V |
| GND | VAUX | 3.3 V |
| VAUX | GND | 4.1 V |
| VAUX | VAUX | 5 V |

When the output voltage drops slightly below the regulated value, the charging current will be enabled as long as VAUX is greater than 2.5 V . Once $\mathrm{V}_{\text {OUT }}$ has reached the proper value, the charging current is turned off.
The internal programmable resistor divider sets $V_{\text {OUT }}$, eliminating the need for very high value external resistors that are susceptible to board leakage.

## OPERATION

In a typical application, a storage capacitor (typically a few hundred microfarads) is connected to $V_{\text {Out }}$. As soon as VAUX exceeds 2.5 V , the $\mathrm{V}_{\text {OUT }}$ capacitor will be allowed to charge up to its regulated voltage. The current available to charge the capacitor will depend on the input voltage and transformer turns ratio, but is limited to about 4.5 mA typical.

## PGOOD

A power good comparator monitors the $\mathrm{V}_{\text {OUT }}$ voltage. The PGD pin is an open-drain output with a weak pull-up ( $1 \mathrm{M} \Omega$ ) to the LDO voltage. Once $\mathrm{V}_{\text {OUT }}$ has charged to within $7.5 \%$ of its regulated voltage, the PGD output will go high. If $\mathrm{V}_{\text {OUT }}$ drops more than $9 \%$ from its regulated voltage, PGD will go low. The PGD output is designed to drive a microprocessor or other chip I/O and is not intended to drive a higher current load such as an LED. Pulling PGD up externally to a voltage greater than VLDO will cause a small current to be sourced into VLDO. PGD can be pulled low in a wire-OR configuration with other circuitry.

## $V_{\text {OUT2 }}$

$V_{\text {OUT2 }}$ is an output that can be turned on and off by the host, using the $V_{\text {OUt2_en }}$ pin. When enabled, $V_{\text {Out2 }}$ is connected to $\mathrm{V}_{\text {OUT }}$ through a $1.3 \Omega$ P-channel MOSFET switch. This output, controlled by a host processor, can be used to power external circuits such as sensors and amplifiers, that do not have a low power sleep or shutdown capability. $V_{\text {OUT2 }}$ can be used to power these circuits only when they are needed.

Minimizing the amount of decoupling capacitance on $V_{\text {OUT2 }}$ will allow it to be switched on and off faster, allowing shorter burst times and, therefore, smaller duty cycles in pulsed applications such as a wireless sensor/transmitter. A small $\mathrm{V}_{\text {OUT2 }}$ capacitor will also minimize the energy that will be wasted in charging the capacitor every time $V_{\text {OUT2 }}$ is enabled.
$V_{\text {OUT2 }}$ has a soft-start time of about $5 \mu$ s to limit capacitor charging current and minimize glitching of the main output when $\mathrm{V}_{\text {OUT2 }}$ is enabled. It also has a current limiting circuit that limits the peak current to 0.3 A typical.

The $\mathrm{V}_{\text {OUT2 }}$ enable input has a typical threshold of 1 V with 100 mV of hysteresis, making it logic-compatible. If $V_{\text {OUT2_EN }}$ (which has an internal pull-down resistor) is low, $V_{\text {OUT2 }}$ will be off. Driving $\mathrm{V}_{\text {OUT2_EN }}$ high will turn on the $V_{\text {out2 }}$ output.
Note that while $\mathrm{V}_{\text {OUT2_EN }}$ is high, the current limiting circuitry for $\mathrm{V}_{\text {OUT2 } 2}$ draws an extra $8 \mu \mathrm{~A}$ of quiescent current from $V_{\text {OUT }}$. This added current draw has a negligible effect on the application and capacitor sizing, since the load on the $\mathrm{V}_{\text {OUT2 }}$ output, when enabled, is likely to be orders of magnitude higher than $8 \mu \mathrm{~A}$.

## VSTORE

The VSTORE output can be used to charge a large storage capacitor or rechargeable battery after $\mathrm{V}_{\text {OUT }}$ has reached regulation. Once $\mathrm{V}_{\text {OUT }}$ has reached regulation, the VSTORE output will be allowed to charge up to the VAUX voltage. The storage element on VSTORE can be used to power the system in the event that the input source is lost, or is unable to provide the current demanded by the $\mathrm{V}_{\text {OUT }}$, $V_{\text {OUT2 }}$ and LDO outputs. If VAUX drops below VSTORE, the LTC3108 will automatically draw current from the storage element. Note that it may take a long time to charge a large capacitor, depending on the input energy available and the loading on $\mathrm{V}_{\text {OUT }}$ and VLDO.
Since the maximum current from VSTORE is limited to a few milliamps, it can safely be used to trickle-charge NiCd or NiMH rechargeable batteries for energy storage when the input voltage is lost. Note that the VSTORE capacitor cannot supply large pulse currents to $\mathrm{V}_{\text {OUT }}$. Any pulse load on $\mathrm{V}_{\text {OUT }}$ must be handled by the $\mathrm{V}_{\text {OUT }}$ capacitor.

## Short-Circuit Protection

All outputs of the LTC3108 are current limited to protect against short-circuits to ground.

## Output Voltage Sequencing

A timing diagram showing the typical charging and voltage sequencing of the outputs is shown in Figure 1. Note: time not to scale.

## operation



Figure 1. Output Voltage Sequencing with $\mathrm{V}_{\text {OUT }}$ Programmed for 3.3 V (Time Not to Scale)

## APPLICATIONS INFORMATION

## Introduction

The LTC3108 is designed to gather energy from very low input voltage sources and convert it to usable output voltages to power microprocessors, wireless transmitters and analog sensors. Such applications typically require much more peak power, and at higher voltages, than the input voltage source can produce. The LTC3108 is designed to accumulate and manage energy over a long period of time to enable short power bursts for acquiring and transmitting data. The bursts must occur at a low enough duty cycle such that the total output energy during the burst does not exceed the average source power integrated over the accumulation time between bursts. For many applications, this time between bursts could be seconds, minutes or hours.

The PGD signal can be used to enable a sleeping microprocessor or other circuitry when $\mathrm{V}_{\text {OUT }}$ reaches regulation, indicating that enough energy is available for a burst.

## Input Voltage Sources

The LTC3108 can operate from a number of low input voltage sources, such as Peltier cells, photovoltaic cells or thermopile generators. The minimum inputvoltage required for a given application will depend on the transformer turns ratio, the load power required, and the internal DC resistance (ESR) of the voltage source. Lower ESR will allow the use of lower input voltages, and provide higher output power capability.

Refer to the $\mathrm{I}_{\mathrm{IN}}$ vs $\mathrm{V}_{\text {IN }}$ curves in the Typical Performance Characteristics section to see what inputcurrent is required from the source for a given input voltage.
For a given transformer turns ratio, there is a maximum recommended input voltage to avoid excessively high secondary voltages and power dissipation in the shunt regulator. It is recommended that the maximum input voltage times the turns ratio be less than 50.
Note that a low ESR bulk decoupling capacitor will usually be required across the input source to prevent large voltage droop and ripple caused by the source's ESR and the peak primary switching current (which can reach hundreds of milliamps). The time constant of the filter capacitor and the ESR of the voltage source should be much longer than the period of the resonant switching frequency.

## Peltier Cell (Thermoelectric Generator)

A Peltier cell (also known as a thermoelectric cooler) is made up of a large number of series-connected $\mathrm{P}-\mathrm{N}$ junctions, sandwiched between two parallel ceramic plates. Although Peltier cells are often used as coolers by applying a DC voltage to their inputs, they will also generate a DC output voltage, using the Seebeck effect, when the two plates are at different temperatures. The polarity of the output voltage will depend on the polarity of the temperature differential between the plates. The magnitude of the output voltage is proportional to the magnitude of the temperature differential between the plates. When used in


Figure 2. Typical Performance of a Peltier Cell Acting as a Thermoelectric Generator

## APPLICATIONS INFORMATION

this manner, a Peltier cell is referred to as a thermoelectric generator (TEG).
The low voltage capability of the LTC3108 design allows it to operate from a TEG with temperature differentials as low as $1^{\circ} \mathrm{C}$, making it ideal for harvesting energy in applications in which a temperature difference exists between two surfaces or between a surface and the ambient temperature. The internal resistance (ESR) of most cells is in the range of $1 \Omega$ to $5 \Omega$, allowing for reasonable power transfer. The curves in Figure 2 show the opencircuit output voltage and maximum power transfer for a typical Peltier cell (with an ESR of $2 \Omega$ ) over a $20^{\circ} \mathrm{C}$ range of temperature differential.

## TEG Load Matching

The LTC3108 was designed to present a minimum input resistance (load) in the range of $2 \Omega$ to $10 \Omega$, depending on input voltage and transformer turns ratio (as shown in the Typical Performance Characteristics curves). For a given turns ratio, as the input voltage drops, the input resistance increases. This feature allows the LTC3108 to optimize power transfer from sources with a few ohms of source resistance, such as a typical TEG. Note that a lower source resistance will always provide more output
current capability by providing a higher input voltage under load.

## Peltier Cell (TEG) Suppliers

Peltier cells are available in a wide range of sizes and power capabilities, from less than 10 mm square to over 50 mm square. They are typically 2 mm to 5 mm in height. A list of Peltier cell manufacturers is given in Table 3.

## Table 3. Peltier Cell Manufacturers

CUI, Inc.
www.cui.com (Distributor)

## Fujitaka

www.fujitaka.com/pub/peltier/english/thermoelectric_power.html
Ferrotec
www.ferrotec.com/products/thermal/modules
Kryotherm
www.kryothermusa.com
Laird Technologies
www.lairdtech.com
Marlow Industries
www.marlow.com
Micropelt
www.micropelt.com
Nextreme
www.nextreme.com
TE Technology
www.tetech.com/Peltier-Thermoelectric-Cooler-Modules.html
Tellurex
www.tellurex.com

Table 4. Recommended TEG Part Numbers by Size

| MANUFACTURER | $\mathbf{1 5 m m} \times \mathbf{1 5 m m}$ | $\mathbf{2 0 m m} \times \mathbf{2 0 m m}$ | $\mathbf{3 0 m m} \times \mathbf{3 0 m m}$ | $\mathbf{4 0 m m} \times \mathbf{4 0 m m}$ |
| :--- | :--- | :--- | :--- | :--- |
| CUI Inc. (Distributor) | CP60133 | CP60233 | CP60333 | CP85438 |
| Ferrotec | $9501 / 031 / 030 \mathrm{~B}$ | $9501 / 071 / 040 \mathrm{~B}$ | $9500 / 097 / 090 \mathrm{~B}$ | $9500 / 127 / 100 \mathrm{~B}$ |
| Fujitaka | FPH13106NC | FPH17106NC | FPH17108AC | FPH112708AC |
| Kryotherm |  |  | TGM-127-1.0-0.8 | LCB-127-1.4-1.15 |
| Laird Technology |  | RC3-8-01 | PT6.7.F2.3030.W6 | PT8.12.F2.4040.TA.W6 |
| Marlow Industries |  | C2-20-0409 | RC6-6-01 | RC12-8-01LS |
| Tellurex | C2-15-0405 | TE-31-1.4-1.15 | TE-71-1.4-1.15 | C2-40-1509 |
| TE Technology | TE-31-1.0-1.3 |  | TE-127-1.4-1.05 |  |

## APPLICATIONS INFORMATION

## Thermopile Generator

Thermopile generators (also called powerpile generators) are made up of a number of series-connected thermocouples enclosed in a metal tube. They are commonly used in gas burner applications to generate a DC output of hundreds of millivolts when exposed to the high temperature of a flame. Typical examples are the Honeywell CQ200 and Q313. These devices have an internal series resistance of less than $3 \Omega$, and can generate as much as 750 mV open-circuit at their highest rated temperature. For applications in which the temperature rise is too high for a solid-state thermoelectric device, a thermopile can be used as an energy source to power the LTC3108. Because of the higher output voltages possible with a thermopile generator, a lower transformer turns ratio can be used (typically 1:20, depending on the application).

## Photovoltaic Cell

The LTC3108 converter can also operate from a single photovoltaic cell (also known as a PV or solar cell) at light levels too low for other low input voltage boost converters to operate. However, many variables will affect the performance in these applications. Light levels can vary over several orders of magnitude and depend on lighting conditions (the type of lighting and indoor versus outdoor). Different types of light (sunlight, incandescent, fluorescent) also have different color spectra, and will produce different output power levels depending on which type of photovoltaic cell is being used (monocrystalline, polycrystalline or thin-film). Therefore, the photovoltaic cell must be chosen for the type and amount of light available. Note that the short-circuit output current from the cell must be at least a few milliamps in order to power the LTC3108 converter

## Non-Boost Applications

The LTC3108 can also be used as an energy harvester and power manager for input sources that do not require boosting. In these applications the step-up transformer can be eliminated.
Any source whose peak voltage exceeds 2.5 V AC or 5 V DC can be connected to the C1 input through a currentlimiting resistor where it will be rectified/peak detected. In
these applications the C2 and SW pins are not used and can be grounded or left open.
Examples of such input sources would be piezoelectric transducers, vibration energy harvesters, low current generators, a stack of low current solar cells or a 60 Hz AC input.
A series resistance of at least $100 \Omega / \mathrm{N}$ should be used to limit the maximum current into the VAUX shunt regulator.

## COMPONENT SELECTION

## Step-Up Transformer

The step-up transformer turns ratio will determine how low the input voltage can be for the converter to start. Using a 1:100 ratio can yield start-up voltages as low as 20 mV . Other factors that affect performance are the DC resistance of the transformer windings and the inductance of the windings. Higher DC resistance will result in lower efficiency. The secondary winding inductance will determine the resonant frequency of the oscillator, according to the following formula.

$$
\text { Frequency }=\frac{1}{2 \bullet \pi \bullet \sqrt{\mathrm{~L}(\sec ) \bullet \mathrm{C}}} \mathrm{~Hz}
$$

Where $L$ is the inductance of the transformer secondary winding and $C$ is the load capacitance on the secondary winding. This is comprised of the input capacitance at pin C2, typically 30pF, in parallel with the transformer secondary winding's shunt capacitance. The recommended resonant frequency is in the range of 10 kHz to 100 kHz . See Table 5 for some recommended transformers.

Table 5. Recommended Transformers

| VENDOR | PART NUMBER |
| :--- | :--- |
| Coilcraft <br> www.coilcraft.com | LPR6235-752SML (1:100 Ratio) |
|  | LPR6235-253PML (1:20 Ratio) |
|  | LPR6235-123QML (1:50 Ratio) |
| Würth | 74488540070 (1:100 Ratio) |
| www.we-online | 74488540120 (1:50 Ratio) |
|  | 74488540250 (1:20 Ratio) |

## APPLICATIONS INFORMATION

## C1 Capacitor

The charge pump capacitor that is connected from the transformer's secondary winding to the C1 pin has an effect on converter input resistance and maximum output current capability. Generally, a minimum value of 1 nF is recommended when operating from very low input voltages using a transformer with a ratio of 1:100. Too large a capacitor value can compromise performance when operating at low input voltage or with high resistance sources. For higher input voltages and lower turns ratios, the value of the $\mathrm{C1}$ capacitor can be increased for higher output current capability. Refer to the Typical Applications schematic examples for the recommended value for a given turns ratio.

## Squegging

Certain types of oscillators, including transformer-coupled oscillators such as the resonant oscillator of the LTC3108, can exhibit a phenomenon called squegging. This term refers to a condition that can occur which blocks or stops the oscillation for a period of time much longer than the period of oscillation, resulting in bursts of oscillation. An example of this is the blocking oscillator, which is designed to squegg to produce bursts of oscillation. Squegging is also encountered in RF oscillators and regenerative receivers.

In the case of the LTC3108, squegging can occur when a charge builds up on the C2 gate coupling capacitor, such that the DC bias point shifts and oscillation is extinguished for a certain period oftime, until the charge on the capacitor bleeds off, allowing oscillation to resume. It is difficult to predict when and if squegging will occur in a given application. While squegging is not harmful, it reduces the average output current capability of the LTC3108.
Squegging can easily be avoided by the addition of a bleeder resistor in parallel with the coupling capacitor on the C 2 pin. Resistor values in the range of 100 k to $1 \mathrm{M} \Omega$ are sufficient to eliminate squegging without having any negative impact on performance. For the 330pF capacitor used for C2 in most applications, a 499k bleeder resistor is recommended. See the Typical Applications schematics for an example.

## Using External Charge Pump Rectifiers

The synchronous charge pump rectifiers in the LTC3108 (connected to the C1 pin) are optimized for operation from very low input voltage sources, using typical transformer step-up ratios between 1:100 and 1:50, and typical C1 charge pump capacitor values less than 10 nF .
Operation from higher input voltage sources (typically 250 mV or greater, under load), allows the use of lower transformer step-up ratios (such as 1:20 and 1:10) and larger C1 capacitor values to provide higher output current capability from the LTC3108. However, due to the resulting increase in rectifier currents and resonant oscillator frequency in these applications, the use of external charge pump rectifiers is recommended for optimal performance.
In applications where the step-up ratio is 1:20 or less, and the C1 capacitor is 10 nF or greater, the C 1 pin should be grounded and two external rectifiers (such as 1N4148 or 1 N914 diodes) should be used. These are available as dual diodes in a single package. Avoid the use of Schottky rectifiers, as their lower forward voltage drop increases the minimum start-up voltage. See the Typical Applications schematics for an example.

## $V_{\text {OUT }}$ and VSTORE Capacitor

For pulsed load applications, the $\mathrm{V}_{\text {Out }}$ capacitor should be sized to provide the necessary current when the load is pulsed on. The capacitor value required will be dictated by the load current, the duration of the load pulse, and the amount of voltage droop the circuit can tolerate. The capacitor must be rated for whatever voltage has been selected for $V_{\text {OUT }}$ by VS1 and VS2.

$$
\mathrm{C}_{\text {OUT }}(\mu \mathrm{F}) \geq \frac{\mathrm{I}_{\mathrm{LOAD}}(\mathrm{~mA}) \cdot \operatorname{tPULSE}(\mathrm{ms})}{\mathrm{V}_{\text {OUT }}(\mathrm{V})}
$$

Note that there must be enough energy available from the input voltage source for $V_{\text {Out }}$ to recharge the capacitor during the interval between load pulses (to be discussed in the next example). Reducing the duty cycle of the load pulse will allow operation with less input energy.

## APPLICATIONS INFORMATION

The VSTORE capacitor may be of very large value (thousands of microfarads or even Farads), to provide holdup at times when the input power may be lost. Note that this capacitor can charge all the way to 5.25 V (regardless of the settings for $V_{\text {OUT }}$ ), so ensure that the holdup capacitor has a working voltage rating of at least 5.5 V at the temperature for which it will be used. The VSTORE capacitor can be sized using the following:

$$
\mathrm{C}_{\text {STORE }} \geq \frac{\left[6 \mu \mathrm{~A}+\mathrm{I}_{\mathrm{Q}}+\mathrm{I}_{\mathrm{LDO}}+\left(\mathrm{l}_{\mathrm{BURST}} \bullet \mathrm{t} \bullet \mathrm{f}\right)\right] \bullet \mathrm{TSTORE}}{5.25-\mathrm{V}_{\text {OUT }}}
$$

Where $6 \mu \mathrm{~A}$ is the quiescent current of the LTC3108, $\mathrm{I}_{Q}$ is the load on $\mathrm{V}_{\text {OUT }}$ in between bursts, $\mathrm{I}_{\text {LDO }}$ is the load on the LDO between bursts, IBURST is the total load during the burst, t is the duration of the burst, f is the frequency of the bursts, TSTORE is the storage time required and $\mathrm{V}_{\text {OUT }}$ is the output voltage required. Note that for a programmed output voltage of 5 V , the VSTORE capacitor cannot provide any beneficial storage time.
To minimize losses and capacitor charge time, all capacitors used for $V_{\text {OUT }}$ and VSTORE should be low leakage. See Table 6 for recommended storage capacitors.
Table 6. Recommended Storage Capacitors

| VENDOR | PART NUMBER/SERIES |
| :--- | :--- |
| AVX <br> www.avx.com | BestCap Series |
| TAJ and TPS Series Tantalum |  |
| Cap-XX <br> www.cap-xx.com | GZ Series |
| Cooper/Bussmann <br> www.bussmann.com/3/PowerStor.html | KR Series <br> P Series |
| Vishay/Sprague <br> www.vishay.com/capacitors | Tantamount 592D |
| 595D Tantalum |  |
| 150CRZ/153CRV Aluminum |  |
| 013 RLC (Low Leakage) |  |

Storage capacitors requiring voltage balancing are not recommended due to the current draw of the balancing resistors.

## PCB Layout Guidelines

Due to the rather low switching frequency of the resonant converter and the low power levels involved, PCB layout is not as critical as with many other $D C / D C$ converters. There are, however, a number of things to consider.

Due to the very low input voltage the circuit may operate from, the connections to $\mathrm{V}_{\mathrm{IN}}$, the primary of the transformer and the SW and GND pins of the LTC3108 should be designed to minimize voltage drop from stray resistance and able to carry currents as high as 500 mA . Any small voltage drop in the primary winding conduction path will lower efficiency and increase capacitor charge time.
Also, due to the low charge currents available at the outputs of the LTC3108, any sources of leakage current on the output voltage pins must be minimized. An example board layout is shown in Figure 3.


- VIAS TO GROUND PLANE

Figure 3. Example Component Placement for Two-Layer PC Board (DFN Package)

## Design Example 1

This design example will explain how to calculate the necessary storage capacitor value for $\mathrm{V}_{\text {Out }}$ in pulsed load applications, such as a wireless sensor/transmitter. Inthese types of applications, the load is very small for a majority of the time (while the circuitry is in a low power sleep state), with bursts of load current occurring periodically during a transmit burst. The storage capacitor on $\mathrm{V}_{\text {OUT }}$ supports the load during the transmit burst, and the long sleep time between bursts allows the LTC3108 to recharge the capacitor. A method for calculating the maximum rate

## APPLICATIONS INFORMATION

at which the load pulses can occur for a given output current from the LTC3108 will also be shown.

In this example, $\mathrm{V}_{\text {OUt }}$ is set to 3.3 V , and the maximum allowed voltage droop during a transmit burst is $10 \%$, or 0.33 V . The duration of a transmit burst is 1 ms , with a total average current requirement of 40 mA during the burst. Given these factors, the minimum required capacitance on $V_{\text {OUT }}$ is:

$$
\mathrm{C}_{\text {OUT }}(\mu \mathrm{F}) \geq \frac{40 \mathrm{~mA} \cdot 1 \mathrm{~ms}}{0.33 \mathrm{~V}}=121 \mu \mathrm{~F}
$$

Note that this equation neglects the effect of capacitor ESR on output voltage droop. For most ceramic or low ESR tantalum capacitors, the ESR will have a negligible effect at these load currents.

A standard value of $150 \mu \mathrm{~F}$ or larger could be used for $\mathrm{C}_{0}$ UT in this case. Note that the load current is the total current draw on $\mathrm{V}_{\text {OUT }}, \mathrm{V}_{\text {OUT2 }}$ and VLDO, since the current for all of these outputs must come from $\mathrm{V}_{\text {Out }}$ during a burst. Current contribution from the holdup capacitor on VSTORE is not considered, since it may not be able to recharge between bursts. Also, it is assumed that the charge current from the LTC3108 is negligible compared to the magnitude of the load current during the burst.
To calculate the maximum rate at which load bursts can occur, determine how much charge current is available from the LTC3108 $\mathrm{V}_{\text {OUT }}$ pin given the input voltage source being used. This number is best found empirically, since there are many factors affecting the efficiency of the converter. Also determine what the total load current is on $\mathrm{V}_{\text {out }}$ during the sleep state (between bursts). Note that this must include any losses, such as storage capacitor leakage.
Assume, for instance, that the charge current from the LTC3108 is $50 \mu \mathrm{~A}$ and the total current drawn on $\mathrm{V}_{\text {OUT }}$ in the sleep state is $17 \mu \mathrm{~A}$, including capacitor leakage. In addition, use the value of $150 \mu \mathrm{~F}$ for the $\mathrm{V}_{\text {OUT }}$ capacitor. The maximum transmit rate (neglecting the duration of the transmit burst, which is typically very short) is then given by:

$$
\mathrm{t}=\frac{150 \mu \mathrm{~F} \cdot 0.33 \mathrm{~V}}{(50 \mu \mathrm{~A}-17 \mu \mathrm{~A})}=1.5 \mathrm{sec} \text { or } \mathrm{f}_{\mathrm{MAX}}=0.666 \mathrm{~Hz}
$$

Therefore, in this application example, the circuit can support a 1 ms transmit burst every 1.5 seconds.
It can be determined that for systems that only need to transmit every few seconds (or minutes or hours), the average charge current required is extremely small, as long as the sleep current is low. Even if the available charge current in the example above was only $10 \mu \mathrm{~A}$ and the sleep current was only $5 \mu \mathrm{~A}$, it could still transmit a burst every ten seconds.

The following formula enables the user to calculate the time it will take to charge the LDO output capacitor and the $\mathrm{V}_{\text {OUT }}$ capacitor the first time, from OV . Here again, the charge current available from the LTC3108 must be known. For this calculation, it is assumed that the LDO output capacitor is $2.2 \mu \mathrm{~F}$.

$$
\mathrm{t}_{\mathrm{LDO}}=\frac{2.2 \mathrm{~V} \cdot 2.2 \mu \mathrm{~F}}{\mathrm{I}_{\mathrm{CHG}}-\mathrm{I}_{\mathrm{LDO}}}
$$

If there were $50 \mu \mathrm{~A}$ of charge current available and a $5 \mu \mathrm{~A}$ load on the LDO (when the processor is sleeping), the time for the LDO to reach regulation would be 107 ms .
If $\mathrm{V}_{\text {OUT }}$ were programmed to 3.3 V and the $\mathrm{V}_{\text {OUT }}$ capacitor was $150 \mu \mathrm{~F}$, the time for $\mathrm{V}_{\text {OUT }}$ to reach regulation would be:

$$
\mathrm{t}_{\text {VOUT }}=\frac{3.3 \mathrm{~V} \cdot 150 \mu \mathrm{~F}}{\mathrm{I}_{\text {CHG }}-\mathrm{I}_{\text {VOUT }}-\mathrm{I}_{\text {LDO }}}+\mathrm{t}_{\mathrm{LDO}}
$$

If there were $50 \mu \mathrm{~A}$ of charge current available and $5 \mu \mathrm{~A}$ of load on $\mathrm{V}_{\text {OUT }}$, the time for $\mathrm{V}_{\text {OUT }}$ to reach regulation after the initial application of power would be 12.5 seconds.

## Design Example 2

In many pulsed load applications, the duration, magnitude and frequency of the load current bursts are known and fixed. In these cases, the average charge current required from the LTC3108 to support the average load must be calculated, which can be easily done by the following:

$$
I_{C H G} \geq I_{Q}+\frac{I_{B U R S T} \bullet t}{T}
$$

Where $\mathrm{I}_{\mathrm{Q}}$ is the sleep current on $\mathrm{V}_{\text {OUT }}$ required by the external circuitry in between bursts (including cap leakage), $I_{\text {BURST }}$ is the total load current during the burst, t is the

## APPLICATIONS INFORMATION

duration of the burst and $T$ is the period of the transmit burst rate (essentially the time between bursts).
In this example, $I_{Q}=5 \mu A, I_{\text {BURST }}=100 \mathrm{~mA}, t=5 \mathrm{~ms}$ and $\mathrm{T}=$ one hour. The average charge current required from the LTC3108 would be:

$$
\mathrm{I}_{\mathrm{CHG}} \geq 5 \mu \mathrm{~A}+\frac{100 \mathrm{~mA} \cdot 0.005 \mathrm{sec}}{3600 \mathrm{sec}}=5.14 \mu \mathrm{~A}
$$

Therefore, if the LTC3108 has an input voltage that allows it to supply a charge current greater than $5.14 \mu \mathrm{~A}$, the application can support 100 mA bursts lasting 5 ms every
hour. It can be determined that the sleep current of $5 \mu \mathrm{~A}$ is the dominant factor because the transmit duty cycle is so small $(0.00014 \%)$. Note that for a $V_{\text {OUT }}$ of 3.3 V , the average power required by this application is only $17 \mu \mathrm{~W}$ (not including converter losses).
Note that the charge current available from the LTC3108 has no effect on the sizing of the $V_{\text {OUT }}$ capacitor (if it is assumed that the load current during a burst is much larger than the charge current), and the $\mathrm{V}_{\text {OUT }}$ capacitor has no effect on the maximum allowed burst rate.

## TYPICAL APPLICATIONS

Peltier-Powered Energy Harvester for Remote Sensor Applications


## TYPICAL APPLICATIONS

Li-Ion Battery Charger and LDO Powered by a Solar Cell


Supercapacitor Charger and LDO Powered by a Thermopile Generator


## DC Input Energy Harvester and Power Manager



AC Input Energy Harvester and Power Manager


## PACKAGE DESCRIPTION

Please refer to http://www.linear.com/designtools/packaging/ for the most recent package drawings.

## GN Package

16-Lead Plastic SSOP (Narrow . 150 Inch)
(Reference LTC DWG \# 05-08-1641 Rev B)

*DIMENSION DOES NOT INCLUDE MOLD FLASH. MOLD FLASH SHALL NOT EXCEED $0.006{ }^{\prime \prime}(0.152 \mathrm{~mm})$ PER SIDE
*DIMENSION DOES NOT INCLUDE INTERLEAD FLASH. INTERLEAD FLASH SHALL NOT EXCEED 0.010" ( 0.254 mm ) PER SIDE

DE/UE Package
12-Lead Plastic DFN ( $4 \mathrm{~mm} \times 3 \mathrm{~mm}$ )
(Reference LTC DWG \# 05-08-1695 Rev D)


RECOMMENDED SOLDER PAD PITCH AND DIMENSIONS APPLY SOLDER MASK TO AREAS THAT ARE NOT SOLDERED


NOTE:

1. DRAWING PROPOSED TO BE A VARIATION OF VERSION (WGED) IN JEDEC PACKAGE OUTLINE M0-229
2. DRAWING NOT TO SCALE
3. ALL DIMENSIONS ARE IN MILLIMETERS
4. DIMENSIONS OF EXPOSED PAD ON BOTTOM OF PACKAGE DO NOT INCLUDE

MOLD FLASH. MOLD FLASH, IF PRESENT, SHALL NOT EXCEED 0.15 mm ON ANY SIDE
5. EXPOSED PAD SHALL BE SOLDER PLATED
6. SHADED AREA IS ONLY A REFERENCE FOR PIN 1 LOCATION ON THE TOP AND BOTTOM OF PACKAGE

## REVISION HISTORY

| REV | DATE | DESCRIPTION | PAGE NUMBER |
| :---: | :---: | :--- | :---: |
| A | $04 / 10$ | Updated front page text and Typical Appliction | 1 |
|  |  | Updated Absolute Maximum Ratings and Order Information sections  <br>   <br>   <br>  Updated Electrical Characteristics <br> Added graph (3108 GOO) to Typical Performance Characteristics 2 <br>   <br>   <br>  Updated Block Diagram <br>  Text added to Operation section <br>  Changes to Applications Information section <br>  Updated Typical Applications <br>  Updated Related Parts | 3 |
|  | B | $06 / 13$ | Added vendor information to Table 5 |
| C | $08 / 13$ | Changed Würth transformer part numbers | 4 |

## LTC3108

## TYPICAL APPLICATION

Dual TEG Energy Harvester Operates from Temperature Differentials of Either Polarity


## reLated parts

| PART NUMBER | DESCRIPTION | COMMENTS |
| :---: | :---: | :---: |
| LTC1041 | Bang-Bang Controller | $\mathrm{V}_{\text {IN: }}$ : 2.8 V to 16V; $\mathrm{I}_{0}=1 \mu \mathrm{~A} ;$ S0-8 Package |
| LTC1389 | Nanopower Precision Shunt Voltage Reference | $\mathrm{V}_{\text {OUT(MIN) }}=1.25 \mathrm{~V}$; $\mathrm{I}_{\mathrm{Q}}=0.8 \mu \mathrm{~A}$; S0-8 Package |
| $\begin{aligned} & \text { LT1672/LT1673/ } \\ & \text { LT1674 } \end{aligned}$ | Single-/Dual-/Quad-Precision $2 \mu$ A Rail-to-Rail Op Amps | SO-8, SO-14 and MSOP-8 Packages |
| LT3009 | $3 \mu \mathrm{~A} \mathrm{I}_{\mathrm{Q}}, 20 \mathrm{~mA}$ Linear Regulator | $\mathrm{V}_{\text {IN: }} 1.6 \mathrm{~V}$ to 20 V ; $\mathrm{V}_{\text {OUT(MII) }}$ : 0.6 V to Adj, $1.2 \mathrm{~V}, 1.5 \mathrm{~V}, 1.8 \mathrm{~V}, 2.5 \mathrm{~V}, 3.3 \mathrm{~V}$, 5 V to Fixed; $\mathrm{I}_{\mathrm{Q}}=3 \mu \mathrm{~A} ; \mathrm{I}_{\mathrm{SD}}<1 \mu \mathrm{~A} ; 2 \mathrm{~mm} \times 2 \mathrm{~mm}$ DFN-8 and SC70 Packages |
| LTC3108-1 | Ultralow Voltage Step-Up Converter and Power Manager | $\mathrm{V}_{\text {IN: }}: 0.02 \mathrm{~V}$ to $1 \mathrm{~V} ; \mathrm{V}_{\text {OUT }}=2.5 \mathrm{~V}, 3 \mathrm{~V}, 3.7 \mathrm{~V}, 4.5 \mathrm{~V}$ Fixed; $\mathrm{I}_{\mathrm{Q}}=6 \mu \mathrm{~A}$; $3 \mathrm{~mm} \times 4 \mathrm{~mm}$ DFN-12 and SSOP-16 Packages |
| $\begin{aligned} & \text { LTC3525L-3/ } \\ & \text { LTC3525L-3.3/ } \\ & \text { LTC3525L-5 } \end{aligned}$ | 400mA (Isw), Synchronous Step-Up DC/DC Converter with Output Disconnect | $\mathrm{V}_{\text {IN }}: 0.7 \mathrm{~V}$ to $4 \mathrm{~V} ; \mathrm{V}_{\text {OUT(MIN }}=5 \mathrm{~V}_{\text {MAX }} ; \mathrm{I}_{\mathrm{Q}}=7 \mu \mathrm{~A} ; \mathrm{I}_{\text {SD }}<1 \mu \mathrm{~A} ;$ SC70 Package |
| LTC3588-1 | Piezoelectric Energy Generator with Integrated High Efficiency Buck Converter | $\mathrm{V}_{\text {IN: }}$ : 2.7 V to 20V; $\mathrm{V}_{\text {OUt(min): }}$ Fixed to $1.8 \mathrm{~V}, 2.5 \mathrm{~V}, 3.3 \mathrm{~V}, 3.6 \mathrm{~V} ; \mathrm{I}_{\mathrm{Q}}=0.95 \mathrm{\mu A}$; $3 \mathrm{~mm} \times 3 \mathrm{~mm}$ DFN-10 and MSOP-10E Packages |
| LTC3642 | 45V, 50mA Synchronous MicroPower Buck Converter | $\mathrm{V}_{\text {IN: }}: 4.5 \mathrm{~V}$ to $45 \mathrm{~V}, 60 \mathrm{~V}_{\text {Max }}$; $\mathrm{V}_{\text {OUT(MIN) }}$ : 0.8 V to Adj, 3.3V Fixed, 5 V Fixed; $I_{Q}=12 \mu A ; I_{S D}<1 \mu A ; 3 \mathrm{~mm} \times 3 \mathrm{~mm}$ DFN-8 and MSOP-8E Packages |
| LTC6656 | 850mA Precision Reference | Series Low Dropout Precision |
| LT8410/ LT8410-1 | MicroPower 25mA/8mA Low Noise Boost Converter with Integrated Schottky Diode and Output Disconnect | $\mathrm{V}_{\text {IN: }}: 2.6 \mathrm{~V}$ to $16 \mathrm{~V} ; \mathrm{V}_{\text {OUT(MIN }}=40 \mathrm{~V}_{\text {MAX }} ; \mathrm{I}_{\mathrm{O}}=8.5 \mu \mathrm{~A} ; \mathrm{I}_{\mathrm{SD}}<1 \mu \mathrm{~A}$; $2 \mathrm{~mm} \times 2 \mathrm{~mm}$ DFN-8 Package |
| LTC4070 | Micropower Shunt Li-Ion Charge | Controls Charging with $\mu \mathrm{A}$ Source |

Appendix C

Datasheet LTC3109

## Auto-Polarity, Ultralow Voltage Step-Up Converter and Power Manager DESCRIPTION

The LTC ${ }^{\circledR} 109$ is a highly integrated DC/DC converter ideal for harvesting surplus energy from extremely low input voltage sources such as TEGs (thermoelectric generators) and thermopiles. Its unique, proprietary autopolarity topology* allows it to operate from input voltages as low as 30 mV , regardless of polarity.

Using two compact step-up transformers and external energy storage elements, the LTC3109 provides a complete power management solution for wireless sensing and data acquisition. The 2.2V LDO can power an external microprocessor, while the main output can be programmed to one of four fixed voltages. The power good indicator signals that the main output is within regulation. A second output can be enabled by the host. A storage capacitor (or battery) can also be charged to provide power when the input voltage source is unavailable. Extremely low quiescent current and high efficiency maximizes the harvested energy available for the application.

The LTC3109 is available in a small, thermally enhanced 20 -lead ( $4 \mathrm{~mm} \times 4 \mathrm{~mm}$ ) QFN package and a 20 -lead SSOP package.

[^5]TYPICAL APPLICATION


## ABSOLUTG MAXIMUM RATINGS (Note 1)

| SWA, SWB, $\mathrm{V}_{\text {INA }}$, V $\mathrm{INB}^{\text {V Voltage } . . . . . . . . . . . . . . . . . . ~}-0$ | VLDO, VSTORE ...................................... -0.3 V to 6V |
| :---: | :---: |
| C1A, C1B Voltage ................................... -0.3 V to 6V | VAUX............................................. 15m |
| C2A, C2B Voltage (Note 6)......................... -8 V to 8V | Operating Junction Temperature Range |
|  | (Note 2).......................................... $40^{\circ} \mathrm{C}$ to $125^{\circ} \mathrm{C}$ |
| VS1, VS2, V OUT $^{\text {, PGOOD }}$.......................... -0.3 V to 6V | Storage Temperature Range ................ $-65^{\circ} \mathrm{C}$ to $125^{\circ} \mathrm{C}$ |

## PIn CONFIGURATION



## ORDER INFORMATION

| LEAD FREE FINISH | TAPE AND REEL | PART MARKING* | PACKAGE DESCRIPTION | TEMPERATURE RANGE |
| :--- | :--- | :--- | :--- | :--- |
| LTC3109EUF\#PBF | LTC3109EUF\#TRPBF | 3109 | $20-$ Lead $(4 \mathrm{~mm} \times 4 \mathrm{~mm})$ Plastic QFN | $-40^{\circ} \mathrm{C}$ to $125^{\circ} \mathrm{C}$ |
| LTC3109IUF\#PBF | LTC3109IUF\#TRPBF | 3109 | $20-$ Lead ( $4 \mathrm{~mm} \times 4 \mathrm{~mm}$ ) Plastic QFN | $-40^{\circ} \mathrm{C}$ to $125^{\circ} \mathrm{C}$ |
| LTC3109EGN\#PBF | LTC3109EGN\#TRPBF | LTC3109GN | 20-Lead Plastic SSOP | $-40^{\circ} \mathrm{C}$ to $125^{\circ} \mathrm{C}$ |
| LTC3109IGN\#PBF | LTC3109IGN\#TRPBF | LTC3109GN | $20-$ Lead Plastic SSOP | $-40^{\circ} \mathrm{C}$ to $125^{\circ} \mathrm{C}$ |

Consult LTC Marketing for parts specified with wider operating temperature ranges. *The temperature grade is identified by a label on the shipping container. Consult LTC Marketing for information on non-standard lead based finish parts.
For more information on lead free part marking, go to: http://www.linear.com/leadfree/
For more information on tape and reel specifications, go to: http://www.linear.com/tapeandreel/

ELECTRICAL CHARACTERISTICS The • denotes the specifications which apply over the full operating junction temperature range, otherwise specifications are for $\mathrm{T}_{\mathrm{A}}=25^{\circ} \mathrm{C}$ (Note 2). VAUX $=5 \mathrm{~V}$ unless otherwise noted.

| PARAMETER | CONDITIONS |  | MIN | TYP | MAX | UNITS |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Minimum Start-Up Voltage | Using 1:100 Transformer Turns Ratio, VAUX = OV |  |  | $\pm 30$ | $\pm 50$ | mV |
| No-Load Input Current | Using 1:100 Transformer Turns Ratios, <br> $\mathrm{V}_{\text {IN }}=30 \mathrm{mV}$, $\mathrm{V}_{\text {OUT2_EN }}=$ OV, All Outputs Charged and in Regulation |  |  | 6 |  | mA |
| Input Voltage Range | Using 1:100 Transformer Turns Ratios | $\bullet$ | $V_{\text {STARTUP }}$ |  | $\pm 500$ | mV |
| Output Voltage | $\begin{aligned} & \text { VS1 = VS2 = GND } \\ & \text { VS1 = VAUX, VS2 = GND } \\ & \text { VS1 = GND, VS2 = VAUX } \\ & \text { VS1 = VS2 = VAUX } \end{aligned}$ |  | $\begin{aligned} & \hline 2.30 \\ & 3.234 \\ & 4.018 \\ & 4.875 \end{aligned}$ | $\begin{aligned} & 2.350 \\ & 3.300 \\ & 4.100 \\ & 5.000 \end{aligned}$ | $\begin{gathered} \hline 2.40 \\ 3.366 \\ 4.182 \\ 5.10 \end{gathered}$ | V V V V |
| VAUX Quiescent Current | No Load, All Outputs Charged |  |  | 7 | 10 | $\mu \mathrm{A}$ |
| VAUX Clamp Voltage | Current Into VAUX $=5 \mathrm{~mA}$ | $\bullet$ | 5.0 | 5.25 | 5.55 | V |
| $V_{\text {OUT }}$ Quiescent Current | $\mathrm{V}_{\text {OUT }}=3.3 \mathrm{~V}, \mathrm{~V}_{\text {OUT2_EN }}=0 \mathrm{~V}$ |  |  | 0.2 |  | $\mu \mathrm{A}$ |
| $\mathrm{V}_{\text {OUT }}$ Current Limit | $\mathrm{V}_{\text {OUT }}=0 \mathrm{~V}$ | $\bullet$ | 6 | 15 | 26 | mA |
| N-Channel MOSFET On-Resistance | $\mathrm{C} 2 \mathrm{~B}=\mathrm{C} 2 \mathrm{~A}=5 \mathrm{~V}$ (Note 3) Measured from $\mathrm{V}_{\text {INA }}$ or SWA, VINB or SWB to GND |  |  | 0.35 |  | $\Omega$ |
| LDO Output Voltage | 0.5 mA Load On V LDO | $\bullet$ | 2.134 | 2.2 | 2.30 | V |
| LDO Load Regulation | For OmA to 2mA Load |  |  | 0.5 | 1 | \% |
| LDO Line Regulation | For $\mathrm{V}_{\text {AUX }}$ from 2.5 V to 5 V |  |  | 0.05 | 0.2 | \% |
| LDO Dropout Voltage | $\mathrm{I}_{\text {LDO }}=2 \mathrm{~mA}$ | $\bullet$ |  | 100 | 200 | mV |
| LDO Current Limit | $\mathrm{V}_{\text {LDO }}=0 \mathrm{~V}$ | $\bullet$ | 5 | 12 |  | mA |
| VSTORE Leakage Current | VSTORE $=5 \mathrm{~V}$ |  |  | 0.1 | 0.3 | $\mu \mathrm{A}$ |
| VSTORE Current Limit | VSTORE $=0 \mathrm{~V}$ | $\bullet$ | 6 | 15 | 26 | mA |
| $\mathrm{V}_{\text {OUT2 }}$ Leakage Current | $\mathrm{V}_{\text {OUT2 }}=$ OV, $\mathrm{V}_{\text {OUT2_EN }}=0 \mathrm{~V}$ |  |  | 50 |  | nA |
| VS1, VS2 Threshold Voltage |  | $\bullet$ | 0.4 | 0.85 | 1.2 | V |
| VS1, VS2 Input Current | $V_{S 1}=V_{S 2}=5 \mathrm{~V}$ |  |  | 1 | 50 | nA |
| PGOOD Threshold (Rising) | Measured Relative to the $\mathrm{V}_{\text {Out }}$ Voltage |  |  | -7.5 |  | \% |
| PGOOD Threshold (Falling) | Measured Relative to the $\mathrm{V}_{\text {OUT }}$ Voltage |  |  | -9 |  | \% |
| PGOOD V ${ }_{\text {OL }}$ | Sink Current $=100 \mu \mathrm{~A}$ |  |  | 0.12 | 0.3 | V |
| PGOOD $\mathrm{V}_{\text {OH }}$ | Source Current = 0 |  | 2.1 | 2.2 | 2.3 | V |
| PGOOD Pull-Up Resistance |  |  |  | 1 |  | $\mathrm{M} \Omega$ |
| $\mathrm{V}_{\text {OUT2_EN }}$ Threshold Voltage | Vout2_EN Rising | $\bullet$ | 0.4 | 1.0 | 1.3 | V |
| $\mathrm{V}_{\text {OUT2_EN }}$ Threshold Hysteresis |  |  |  | 100 |  | mV |
| $\mathrm{V}_{\text {OUT2_EN }}$ Pull-Down Resistance |  |  |  | 5 |  | $\mathrm{M} \Omega$ |
| $V_{\text {Out2 }}$ Turn-On Time |  |  |  | 0.5 |  | $\mu \mathrm{S}$ |
| $V_{\text {Out2 }}$ Turn-Off Time | (Note 3) |  |  | 0.15 |  | $\mu \mathrm{S}$ |
| $V_{\text {OUT2 }}$ Current Limit | $\mathrm{V}_{\text {OUT }}=3.3 \mathrm{~V}$ | $\bullet$ | 0.2 | 0.3 | 0.5 | A |
| $\mathrm{V}_{\text {OUT2 }}$ Current Limit Response Time | (Note 3) |  |  | 350 |  | ns |
| $\mathrm{V}_{\text {OUT2 }} \mathrm{P}$-Channel MOSFET On-Resistance | $\mathrm{V}_{\text {OUT }}=5 \mathrm{~V}$ (Note 3) |  |  | 1.0 |  | $\Omega$ |

Note 1: Stresses beyond those listed under Absolute Maximum Ratings may cause permanent damage to the device. Exposure to any Absolute Maximum Rating condition for extended periods may affect device reliability and lifetime.
Note 2: The LTC3109 is tested under pulsed load conditions such that $T_{J} \approx T_{A}$. The LTC3109E is guaranteed to meet specifications from
$0^{\circ} \mathrm{C}$ to $85^{\circ} \mathrm{C}$ junction temperature. Specifications over the $-40^{\circ} \mathrm{C}$ to $125^{\circ} \mathrm{C}$ operating junction temperature range are assured by design, characterization and correlation with statistical process controls. The LTC3109I is guaranteed over the full $-40^{\circ} \mathrm{C}$ to $125^{\circ} \mathrm{C}$ operating junction temperature range. Note that the maximum ambient temperature is determined by specific operating conditions in conjunction with

## eLECTRICAL CHARACTERISTICS

board layout, the rated thermal package thermal resistance and other environmental factors. The junction temperature ( $\mathrm{T}_{\mathrm{J}}$ ) is calculated from the ambient temperature $\left(\mathrm{T}_{\mathrm{A}}\right)$ and power dissipation $\left(\mathrm{P}_{\mathrm{D}}\right)$ according to the formula: $T_{J}=T_{A}+\left(P_{D} \cdot \theta_{J A}{ }^{\circ} C / W\right)$, where $\theta_{J A}$ is the package thermal impedance.
Note 3: Specification is guaranteed by design and not $100 \%$ tested in production.
Note 4: Current measurements are made when the output is not switching.

Note 5: Failure to solder the exposed backside of the QFN package to the PC board ground plane will result in a thermal resistance much higher than $37^{\circ} \mathrm{C} / \mathrm{W}$.
Note 6: The Absolute Maximum Rating is a DC rating. Under certain conditions in the applications shown, the peak AC voltage on the C2A and C2B pins may exceed $\pm 8 V$. This behavior is normal and acceptable because the current into the pin is limited by the impedance of the coupling capacitor.

## TYPICAL PERFORMANC $\in$ CHARACT $\in$ RISTICS $\mathrm{T}_{A}=25^{\circ}$., unless otherwise noted.



LIEAR

TYPICAL PERFORMAOCE CHARACTERISTICS $\mathrm{T}_{\mathrm{A}}=25^{\circ}$, unless otherwise noted.


Resonant Switching Waveforms



LDO Load Regulation

$V_{\text {OUT }}$ and PGOOD Response
During a Step Load


Pvout vs dT and TEG Size, $1: 100$ Ratio, $V_{\text {OUT }}=5 \mathrm{~V}$


3109608
LDO Dropout Voltage

$V_{\text {OUT }}$ Ripple


TYPICAL PERFORMANCE CHARACTERISTICS $\mathrm{T}_{\mathrm{A}}=25^{\circ}$, unless otherwise noted.


## PIn functions afn/ssopl

VSTORE (Pin 1/Pin 3): Output for the Storage Capacitor or Battery. A large storage capacitor may be connected from this pin to GND for powering the system in the event the input voltage is lost. It will be charged up to the maximum VAUX clamp voltage. If not used, this pin should be left open or tied to VAUX.
VAUX (Pin 2/Pin 4): Output of the Internal Rectifier Circuit and $V_{\text {CC }}$ for the IC. Bypass VAUX with at least $1 \mu \mathrm{~F}$ of capacitance to ground. An active shunt regulator clamps VAUX to 5.25 V (typical).
$V_{\text {OUt }}$ (Pin 3/Pin 5): Main Output of the Converter. The voltage at this pin is regulated to the voltage selected by VS1 and VS2 (see Table 1). Connect this pin to a reservoir capacitor or to a rechargeable battery. Any high current pulse loads must be fed by the reservoir capacitor on this pin.
$V_{\text {OUT2 }}$ (Pin 4/ Pin 6): Switched Output of the Converter. Connect this pin to a switched load. This output is open until $\mathrm{V}_{\text {OUT_EN }}$ is driven high, then it is connected to $\mathrm{V}_{\text {OUT }}$ through a $1 \Omega$ PMOS switch. If not used, this pin should be left open or tied to $\mathrm{V}_{\text {Out }}$.
$V_{\text {OUt2_en }}$ (Pin 5/Pin 7): Enable Input for $\mathrm{V}_{\text {Out2. }}$ V $\mathrm{V}_{\text {OUT2 }}$ will be enabled when this pin is driven high. There is an internal 5 M pull-down resistor on this pin. If not used, this pin can be left open or grounded.

PGOOD (Pin 6/Pin 8): Power Good Output. When Vout is within $7.5 \%$ of its programmed value, this pin will be pulled up to the LDO voltage through a 1M resistor. If $V_{\text {OUT }}$ drops $9 \%$ below its programmed value PGOOD will go low. This pin can sink up to $100 \mu \mathrm{~A}$.

VLDO (Pin 7/Pin 9): Output of the 2.2V LDO. Connect a $2.2 \mu \mathrm{~F}$ or larger ceramic capacitor from this pin to GND. If not used, this pin should be tied to VAUX.
GND (Pins 8, 11, 16, Exposed Pad Pin 21/Pins 10, 13, 18): Ground Pins. Connect these pins directly to the ground plane. The exposed pad serves as a ground connection and as a means of conducting heat away from the die.
VS2 (Pin 20/Pin 2): Vout Select Pin 2. Connect this pin to ground or VAUX to program the output voltage (see Table 1).
VS1 (Pin 19/Pin 1): Vout Select Pin 1. Connect this pin to ground or VAUX to program the output voltage (see Table 1).

Table 1. Regulated Output Voltage Using Pins VS1 and VS2

| VS2 | VS1 | V $_{\text {OUT }}$ |
| :---: | :---: | :---: |
| GND | GND | 2.35 V |
| GND | VAUX | 3.3 V |
| VAUX | GND | 4.1 V |
| VAUX | VAUX | 5.0 V |

## PIn FUnCTIOnS <br> (DFN/SSOP)

C1B (Pin 9/Pin 11): Inputto theCharge Pump and Rectifier Circuit for Channel B. Connect a capacitor from this pin to the secondary winding of the "B" step-up transformer. Seethe Applications Information section for recommended capacitor values.
C1A (Pin 18/Pin 20): Input to the Charge Pump and Rectifier Circuit for Channel A. Connect a capacitor from this pin to the secondary winding of the "A" step-up transformer. See the Applications Information section for recommended capacitor values.
C2B (Pin 10/Pin 12): Input to the Gate Drive Circuit for SWB. Connect a capacitor from this pin to the secondary winding ofthe "B" step-up transformer. See the Applications Information section for recommended capacitor values.

C2A (Pin 17/Pin 19): Input to the Gate Drive Circuit for SWA. Connect a capacitor from this pin to the secondary winding ofthe "A" step-up transformer. See the Applications Information section for recommended capacitor values.

SWA (Pin 15/Pin 17): Connection to the Internal N-Channel Switch for Channel A. Connect this pin to the primary winding of the " A " transformer.
SWB (Pin 12/Pin 14): Connection to the Internal N-Channel Switch for Channel B. Connect this pin to the primary winding of the " $B$ " transformer.
$V_{\text {INA }}$ (Pin 14/Pin 16): Connection to the Internal N-Channel Switch for Channel A. Connect this pin to one side of the input voltage source (see Typical Applications).
$V_{\text {INB }}$ (Pin 13/Pin 15): Connection to the Internal N-Channel Switch for Channel B. Connect this pin to the other side of the input voltage source (see Typical Applications).

## BLOCK DIAGRAM



## OPERATIOी (Refer to the Block Diagram)

The LTC3109 is designed to use two small external step-up transformers to create an ultralow input voltage step-up DC/DC converter and power manager that can operate from input voltages of either polarity. This unique capability enables energy harvesting from thermoelectric generators (TEGs) in applications where the temperature differential across the TEG may be of either (or unknown) polarity. It can also operate from low level AC sources. It is ideally suited for low power wireless sensors and other applications in which surplus energy harvesting is used to generate system power because traditional battery power is inconvenient or impractical.

The LTC3109 is designed to manage the charging and regulation of multiple outputs in a system in which the average power draw is very low, but where periodic pulses of higher load current may be required. This is typical of wireless sensor applications, where the quiescent power draw is extremely low most of the time, except for transmit pulses when circuitry is powered up to make measurements and transmit data.
The LTC3109 can also be used to trickle charge a standard capacitor, super capacitor or rechargeable battery, using energy harvested from a TEG or low level AC source.

## Resonant Oscillator

The LTC3109 utilizes MOSFET switches to form a resonant step-up oscillator that can operate from an input of either polarity using external step-up transformers and small coupling capacitors. This allows it to boost input voltages as low as 30 mV high enough to provide multiple regulated output voltages for powering other circuits. The frequency of oscillation is determined by the inductance of the transformer secondary winding, and is typically in the range of 10 kHz to 100 kHz . For input voltages as low as 30 mV , transformers with a turns ratio of about 1:100 is recommended. For operation from higher input voltages, this ratio can be lower. See the Applications Information section for more information on selecting the transformers.

## Charge Pump and Rectifier

The AC voltage produced on the secondary winding of the transformer is boosted and rectified using an external charge pump capacitor (from the secondary winding to pin C 1 A or C 1 B ) and the rectifiers internal to the LTC3109. The rectifier circuit feeds current into the $V_{\text {AUX }}$ pin, providing charge to the external VAUX capacitor and the other outputs.

## VAUX

The active circuits within the LTC3109 are powered from VAUX, which should be bypassed with a $1 \mu \mathrm{~F}$ minimum capacitor. Once VAUX exceeds 2.5 V , the main $\mathrm{V}_{\text {OUt }}$ is allowed to start charging.
An internal shunt regulator limits the maximum voltage on VAUX to 5.25 V typical. It shunts to ground any excess current into VAUX when there is no load on the converter or the input source is generating more power than is required by the load. This current should be limited to 15 mA max.

## Voltage Reference

The LTC3109 includes a precision, micropower reference, for accurate regulated output voltages. This reference becomes active as soon as VAUX exceeds 2 V .

## Synchronous Rectifiers

Once VAUX exceeds 2V, synchronous rectifiers in parallel with each of the internal rectifier diodes take over the job of rectifying the input voltage at pins C1A and C1B, improving efficiency.

## Low Dropout Linear Regulator (LDO)

The LTC3109 includes a low current LDO to provide a regulated 2.2 V output for powering low power processors or other low power ICs. The LDO is powered by the higher of VAUX or Vout. This enables it to become active as soon as VAUX has charged to 2.3 V , while the

## OPERATIOी (Refer to the Block Diagram)

$V_{\text {OUT }}$ storage capacitor is still charging. In the event of a step load on the LDO output, current can come from the main $\mathrm{V}_{\text {OUT }}$ reservoir capacitor. The LDO requires a $2.2 \mu \mathrm{~F}$ ceramic capacitor for stability. Larger capacitor values can be used without limitation, but will increase the time it takes for all the outputs to charge up. The LDO output is current limited to 5 mA minimum.

## $V_{\text {OUt }}$

The main output voltage on $\mathrm{V}_{\text {OUT }}$ is charged from the VAUX supply, and is user-programmed to one of four regulated voltages using the voltage select pins VS1 and VS2, according to Table 2. Although the logic-threshold voltage for VS1 and VS2 is 0.85 V typical, it is recommended that they be tied to ground or VAUX.

## Table 2

| VS2 | VS1 | V $_{\text {0UT }}$ |
| :---: | :---: | :---: |
| GND | GND | 2.35 V |
| GND | VAUX | 3.3 V |
| VAUX | GND | 4.1 V |
| VAUX | VAUX | 5 V |

When the output voltage drops slightly below the regulated value, the charging current will be enabled as long as VAUX is greater than 2.5 V . Once $\mathrm{V}_{\text {Out }}$ has reached the proper value, the charging current is turned off. The resulting ripple on $\mathrm{V}_{\text {OUT }}$ is typically less than 20 mV peak to peak.
The internal programmable resistor divider, controlled by VS1 and VS2, sets Vout, eliminating the need for very high value external resistors that are susceptible to noise pickup and board leakages.
In a typical application, a reservoir capacitor (typically a few hundred microfarads) is connected to $\mathrm{V}_{\text {Out }}$. As soon as VAUX exceeds 2.5 V , the $\mathrm{V}_{\text {OUt }}$ capacitor will begin to charge up to its regulated voltage. The current available to charge the capacitor will depend on the input voltage and transformer turns ratio, but is limited to about 15 mA typical. Note that for very low input voltages, this current may be in the range of $1 \mu \mathrm{~A}$ to $1000 \mu \mathrm{~A}$.

## PGOOD

A power good comparator monitors the Vout voltage. The PGOOD pin is an open-drain output with a weak pullup ( $1 \mathrm{M} \Omega$ ) to the LDO voltage. Once $V_{\text {OUT }}$ has charged to within $7.5 \%$ of its programmed voltage, the PGOOD output will go high. If $\mathrm{V}_{\text {OUT }}$ drops more than $9 \%$ from its programmed voltage, PGOOD will go low. The PGOOD output is designed to drive a microprocessor or other chip I/O and is not intended to drive a higher current load such as an LED. The PGOOD pin can also be pulled low in a wire-OR configuration with other circuitry.

## $\mathrm{V}_{\text {OUT2 }}$

$V_{\text {OUT2 }}$ is an output that can be turned on and off by the host using the $\mathrm{V}_{\text {OUT2_EN }}$ pin. When enabled, $\mathrm{V}_{\text {OUT2 }}$ is connected to $\mathrm{V}_{\text {Out }}$ through a $1 \Omega$ P-channel MOSFET switch. This output, controlled by a host processor, can be used to power external circuits such as sensors and amplifiers, that don't have a low power "sleep" or shutdown capability. $V_{\text {OUT2 }}$ can be used to power these circuits only when they are needed.

Minimizing the amount of decoupling capacitance on $V_{\text {out2 }}$ enables it to be switched on and off faster, allowing shorter pulse times and therefore smaller duty cycles in applications such as a wireless sensor/transmitter. A small $V_{\text {OUT2 }}$ capacitor will also minimize the energy that will be wasted in charging the capacitor every time $\mathrm{V}_{\text {OUT2 }}$ is enabled.
$V_{\text {OUT2 }}$ has a current limiting circuit that limits the peak current to 0.3A typical.
The $V_{\text {OUT2 }}$ enable input has a typical threshold of 1 V with 100 mV of hysteresis, making it logic compatible. If $V_{\text {OUT2_EN }}$ (which has an internal 5M pull-down resistor) is low, $V_{\text {OUT2 }}$ will be off. Driving $\mathrm{V}_{\text {OUT2_EN }}$ high will turn on the $\mathrm{V}_{\text {OUT2 }}$ output.
Note that while $\mathrm{V}_{\text {OUT2_EN }}$ is high, the current limiting circuitry for $V_{\text {OUT } 2}$ draws an extra $8 \mu \mathrm{~A}$ of quiescent current from $V_{\text {OUT }}$. This added current draw has a negligible effect

## OPERATIO (Refer to the Block Diagram)

on the application and capacitor sizing, since the load on the $V_{\text {OUT2 }}$ output, when enabled, is likely to be orders of magnitude higher than $8 \mu \mathrm{~A}$.

## VSTORE

The VSTORE output can be used to charge a large storage capacitor or rechargeable battery. Once $\mathrm{V}_{\text {OUT }}$ has reached regulation, the VSTORE output will be allowed to charge up to the clamped VAUX voltage ( 5.25 V typical). The storage element on VSTORE can then be used to power the system in the event that the input source is lost, or is unable to provide the current demanded by the $\mathrm{V}_{\text {OUT }}$, $V_{\text {OUT2 } 2}$ and LDO outputs.
If VAUX drops below VSTORE, the LTC3109 will automatically draw current from the storage element. Note that it may take a long time to charge a large storage capacitor, depending on the input energy available and the loading on $\mathrm{V}_{\text {OUt }}$ and VLDO.

Since the maximum charging current available at the VSTORE output is limited to about 15 mA , it can safely be used to trickle charge NiCd or NiMH batteries for energy storage when the input voltage is lost.
Note that VSTORE is not intended to supply high pulse load currents to $\mathrm{V}_{\text {OUt }}$. Any pulse load on $\mathrm{V}_{\text {OUT }}$ must be handled by the $\mathrm{V}_{\text {OUT }}$ reservoir capacitor.

## Short-Circuit Protection

All outputs of the LTC3109 are current limited to protect against short circuits to ground.

## Output Voltage Sequencing

A timing diagram showing the typical charging and voltage sequencing of the outputs is shown in Figure 1. Note that the horizontal (time) axis is not to scale, and is used for illustration purposes to show the relative order in which the output voltages come up.


Figure 1. Output Voltage Sequencing
(with $\mathrm{V}_{\text {OUT }}$ Programmed for 3.3V). Time Not to Scale

## APPLICATIONS IMFORMATION

## INTRODUCTION

The LTC3109 is designed to gather energy from very low input voltage sources and convert it to usable output voltages to power microprocessors, wireless transmitters and analog sensors. Its architecture is specifically tailored to applications where the input voltage polarity is unknown, or can change. This "auto-polarity" capability makes it ideally suited to energy harvesting applications using a TEG whose temperature differential may be of either polarity.

Applications such as wireless sensors typically require much more peak power, and at higher voltages, than the input voltage source can produce. The LTC3109 is designed to accumulate and manage energy over a long period of time to enable short power pulses for acquiring and transmitting data. The pulses must occur at a low enough duty cycle that the total output energy during the pulse does not exceed the average source power integrated over the accumulation time between pulses. For many applications, this time between pulses could be seconds, minutes or hours.

The PGOOD signal can be used to enable a sleeping microprocessor or other circuitry when $V_{\text {OUT }}$ reaches regulation, indicating that enough energy is available for a transmit pulse.

## INPUT VOLTAGE SOURCES

The LTC3109 can operate from a number of low input voltage sources, such as Peltier cells (thermoelectric generators), or low level AC sources. The minimum input voltage required for a given application will depend on the transformer turns ratios, the load power required, and the internal DC resistance (ESR) of the voltage source. Lower ESR sources will allow operation from lower inputvoltages, and provide higher output power capability.

For a given transformer turns ratio, there is a maximum recommended input voltage to avoid excessively high secondary voltages and power dissipation in the shunt regulator. It is recommended that the maximum input voltage times the turns ratio be less than 50.
Note that a low ESR decoupling capacitor may be required acrossa DC input source to preventlarge voltage droop and
ripple caused by the source's ESR and the peak primary switching current (which can reach hundreds of milliamps). Since the input voltage may be of either polarity, a ceramic capacitor is recommended.

## PELTIER CELL (THERMOELECTRIC GENERATOR)

A Peltier cell is made up of a large number of series-connected P-N junctions, sandwiched between two parallel ceramic plates. Although Peltier cells are often used as coolers by applying a DC voltage to their inputs, they will also generatea DC output voltage, using the Seebeck effect, when the two plates are at different temperatures.
When used in this manner, they are referred to as thermoelectric generators (TEGs). The polarity of the output voltage will depend on the polarity of the temperature differential between the TEG plates. The magnitude of the output voltage is proportional to the magnitude of the temperature differential between the plates.

The low voltage capability of the LTC3109 design allows it to operate fromatypical TEG with temperature differentials as low as $1^{\circ} \mathrm{C}$ of either polarity, making it ideal for harvesting energy in applications where a temperature difference exists between two surfaces or between a surface and the ambient temperature. The internal resistance (ESR) of most TEGs is in the range of $1 \Omega$ to $5 \Omega$, allowing for reasonable power transfer. The curves in Figure 2 show the open-circuit output voltage and maximum power transfer for a typical TEG with an ESR of $2 \Omega$, over a $20^{\circ} \mathrm{C}$ range of temperature differential (of either polarity).


Figure 2. Typical Performance of a Peltier Cell Acting as a Power Generator (TEG)

## APPLICATIONS INFORMATION

## TEG LOAD MATCHING

The LTC3109 was designed to present an input resistance (load) in the range of $2 \Omega$ to $10 \Omega$, depending on input voltage, transformerturns ratio and the C1A and C2A capacitor values (as shown in the Typical Performance curves). For a given turns ratio, as the input voltage drops, the input resistance increases. This feature allows the LTC3109 to optimize power transfer from sources with a few Ohms of source resistance, such as a typical TEG. Note that a lower source resistance will always provide more output current capability by providing a higher input voltage under load.

Table 3. Peltier Cell Manufacturers

| CUI Inc |
| :--- |
| www.cui.com |
| Ferrotec |
| www.ferrotec.com/products/thermal/modules/ |
| Fujitaka |
| www.fujitaka.com/pub/peltier/english/thermoelectric_power.html |
| Hi-Z Technology |
| www.hi-z.com |
| Kryotherm |
| www.kryotherm |
| Laird Technologies |
| www.lairdtech.com |
| Micropelt |
| www.micropelt.com |
| Nextreme |
| www.nextreme.com |
| TE Technology |
| www.tetech.com/Peltier-Thermoelectric-Cooler-Modules.html |
| Tellurex |
| www.tellurex.com/ |

## UNIPOLAR APPLICATIONS

The LTC3109 can also be configured to operate from two independent unipolar voltage sources, such as two TEGs in different locations. In this configuration, energy can be harvested from either or both sources simultaneously. See the Typical Applications for an example.
The LTC3109 can also be configured to operate from a single unipolar source, using a single step-up transformer, by ganging its $\mathrm{V}_{\mathrm{IN}}$ and SW pins together. In this manner, it can extract the most energy from very low resistance sources. See Figure 3 for an example of this configuration, along with the performance curves.

## PELTIER CELL (TEG) SUPPLIERS

Peltier cells are available in a wide range of sizes and power capabilities, from less than 10 mm square to over 50 mm square. They are typically 2 mm to 5 mm in height. A list of some Peltier cell manufacturers is given in Table 3 and some recommended part numbers in Table 4.

## COMPONENT SELECTION

## Step-Up Transformer

The turns ratio of the step-up transformers will determine how low the input voltage can be for the converter to start. Due to the auto-polarity architecture, two identical step-up transformers should be used, unless the temperature drop across the TEG is significantly different in one polarity, in which case the ratios may be different.

Table 4. Recommended TEG Part Numbers by Size

| MANUFACTURER | $\mathbf{1 5 m m}$ | $\mathbf{2 0 m m}$ | $\mathbf{3 0 m m}$ | 40mm |
| :--- | :---: | :---: | :---: | :---: |
| CUI Inc. (Distributor) | CP60133 | CP60233 | CP60333 | CP85438 |
| Ferrotec | $9501 / 031 / 030 \mathrm{~B}$ | $9501 / 071 / 040 \mathrm{~B}$ | $9500 / 097 / 090 \mathrm{~B}$ | $9500 / 127 / 100 \mathrm{~B}$ |
| Fujitaka | FPH13106NC | FPH17106NC | FPH17108AC | FPH112708AC |
| Kryotherm |  |  | TGM-127-1.0-0.8 | LCB-127-1.4-1.15 |
| Laird Technology |  |  | PT6.7.F2.3030.W6 | PT8.12.F2.4040.TA.W6 |
| Marlow Industries |  | RC3-8-01 | RC6-6-01 | RC12-8-01LS |
| Tellurex | C2-15-0405 | C2-20-0409 | C2-30-1505 | C2-40-1509 |
| TE Technology | TE-31-1.0-1.3 | TE-31-1.4-1.15 | TE-71-1.4-1.15 | TE-127-1.4-1.05 |

## APPLICATIONS INFORMATION



Figure 3. Unipolar Application

Typical PVout vs dT for Unipolar
Configuration


Typical IVOUT vs $V_{\text {IN }}$ for Unipolar Configuration


Typical Efficiency vs $V_{I N}$ for Unipolar Configuration


Typical Input Current vs $V_{\text {IN }}$ for Unipolar Configuration


Typical $R_{\text {IN }}$ vs $V_{\text {IN }}$ for Unipolar Configuration


3109 F03e

3109 f03d

## APPLICATIONS INFORMATION

Using a 1:100 primary-secondary ratio yields start-up voltages as low as 30 mV . Other factors that affect performance are the resistance of the transformer windings and the inductance of the windings. Higher DC resistance will result in lower efficiency and higher start-up voltages. The secondary winding inductance will determine the resonant frequency of the oscillator, according to the formula below.

$$
\text { Freq }=\frac{1}{2 \bullet \pi \bullet \sqrt{L_{S E C} \bullet C}} H z
$$

where $L_{\text {SEC }}$ is the inductance of one of the secondary windings and $C$ is the load capacitance on the secondary winding. This is comprised of the input capacitance at pin C2A or C2B, typically 70 pF each, in parallel with the transformer secondary winding's shunt capacitance. The recommended resonant frequency is in the range of 10 kHz to 100 kHz . Note that loading will also affect the resonant frequency. See Table 5 for some recommended transformers.

Table 5. Recommended Transformers

| VENDOR | TYPICAL START- <br> UP VOLTAGE | PART NUMBER |
| :--- | :---: | :--- |
| Coilcraft | 25 mV | LPR6235-752SML (1:100 ratio) |
| www.coilcraft.com | 35 mV | LPR6235-123QML (1:50 ratio) |
|  | 85 mV | LPR6235-253PML (1:20 ratio) |
| Würth | 25 mV | 74488540070 (1:100 Ratio) |
| www.we-online | 35 mV | 74488540120 (1:50 Ratio) |
|  | 85 mV | 74488540250 (1:20 Ratio) |

## USING EXTERNAL CHARGE PUMP RECTIFIERS

The synchronous rectifiers in the LTC3109 have been optimized for low frequency, low current operation, typical of low input voltage applications. For applications where the resonant oscillator frequency exceeds 100 kHz , or a transformer turns ratio of less than 1:20 is used, or the C 1 A and C 1 B capacitor values are greater than 68 nF , the use of external charge pump rectifiers (1N4148 or 1N914 or equivalent) is recommended. See the Typical Application circuits for an example. Avoid the use of Schottky rectifiers, as their low forward voltage increases the minimum start-up voltage.

## C1 CAPACITOR

The charge pump capacitor that is connected from each transformer's secondary winding to the corresponding C1A and C1B pins has an effect on converter input resistance and maximum output current capability. Generally a minimum value of 1 nF is recommended when operating from very low input voltages using a transformer with a ratio of $1: 100$. Capacitor values of 2.2 nF to 10 nF will provide higher output current at higher input voltages, however larger capacitor values can compromise performance when operating at low input voltage or with high resistance sources. For higher input voltages and lower turns ratios, the value of the C1 capacitor can be increased for higher output current capability. Refer to the Typical Applications examples for the recommended value for a given turns ratio.

## C2 CAPACITOR

The C2 capacitors connect pins C2A and C2B to their respective transformer secondary windings. For most applications a capacitor value of 470 pF is recommended. Smaller capacitor values tend to raise the minimum start-up voltage, and larger capacitor values can lower efficiency.
Note that the C1 and C2 capacitors must have a voltage rating greater than the maximum input voltage times the transformer turns ratio.

## $V_{\text {OUT }}$ AND VSTORE CAPACITOR

For pulsed load applications, the $\mathrm{V}_{\text {OUT }}$ capacitor should be sized to provide the necessary current when the load is pulsed on. The capacitor value required will be dictated by the load current ( $l_{\text {LOAD }}$ ), the duration of the load pulse (tpULSE), and the amount of $V_{\text {OUT }}$ voltage droop the application can tolerate ( $\Delta \mathrm{V}_{\text {OUT }}$ ). The capacitor must be rated for whatever voltage has been selected for $V_{\text {OUT }}$ by VS1 and VS2:

$$
\mathrm{C}_{\text {OUT }}(\mu \mathrm{F}) \geq \frac{\mathrm{I}_{\mathrm{LOAD}(\mathrm{~mA})} \mathrm{t}_{\text {PULSE }(\mathrm{ms})}}{\Delta \mathrm{V}_{\text {OUT }}(\mathrm{V})}
$$

## APPLICATIONS INFORMATION

Note that there must be enough energy available from the input voltage source for $V_{\text {OUT }}$ to recharge the capacitor during the interval between load pulses (as discussed in Design Example 1). Reducing the duty cycle of the load pulse will allow operation with less input energy.
The VSTORE capacitor may be of very large value (thousands of microfarads or even Farads), to provide energy storage at times when the input voltage is lost. Note that this capacitor can charge all the way to the VAUX clamp voltage of 5.25 V typical (regardless of the settings for $V_{\text {OUt }}$ ), so be sure that the holdup capacitor has a working voltage rating of at least 5.5 V at the temperature that it will be used.

The VSTORE input is not designed to provide high pulse load currents to $\mathrm{V}_{\text {OUT }}$. The current path from VSTORE to $V_{\text {OUT }}$ is limited to about 26 mA max.
The VSTORE capacitor can be sized using the following formula:

$$
\mathrm{C}_{\text {STORE }} \geq \frac{\left(7 \mu \mathrm{~A}+\mathrm{I}_{Q}+\mathrm{I}_{\text {LDO }}+\left(\mathrm{l}_{\text {PULSE }} \bullet \mathrm{t}_{\text {PULSE }} \bullet \mathrm{f}\right)\right) \bullet \mathrm{t}_{\text {STORE }}}{5.25-\mathrm{V}_{\text {OUT }}}
$$

where $7 \mu \mathrm{~A}$ is the quiescent current of the LTC3109, $\mathrm{I}_{\mathrm{Q}}$ is the load on $\mathrm{V}_{\text {OUT }}$ in between pulses, $\mathrm{I}_{\text {LDO }}$ is the load on the LDO between pulses, IPULSE is the total load during the pulse, tpulse is the duration of the pulse, $f$ is the frequency of the pulses, tstore is the total storage time required and $\mathrm{V}_{\text {OUt }}$ is the output voltage required. Note that for a programmed output voltage of 5 V , the VSTORE capacitor cannot provide any beneficial storage time to $V_{\text {OUT }}$.
To minimize losses and capacitor charge time, all capacitors used for $V_{\text {OUT }}$ and VSTORE should be low leakage. See Table 6 for recommended storage capacitors.

Table 6. Recommended Storage Capacitors

| VENDOR | PART NUMBER/SERIES |
| :--- | :--- |
| AVX | BestCap Series |
| www.avx.com | TAJ and TPS Series Tantalum |
| Cap-XX | GZ Series |
| www.cap-xx.com | KR Series |
| Cooper/Bussman | P Series |
| www.bussmann.com/3/PowerStor.html | Tantamount 592D |
| Vishay/Sprague | 595D Tantalum |

Note that storage capacitors requiring voltage balancing resistors are not recommended due to the steady-state current draw of the resistors.

## PCB LAYOUT GUIDELINES

Due to the rather low switching frequency of the resonant converter and the low power levels involved, PCB layout is not as critical as with many other DC/DC converters. There are however, a number of things to consider.
Due to the very low input voltages the circuit operates from, the connections to $\mathrm{V}_{\mathrm{IN}^{\prime}}$, the primary of the transformers and the SW, VIN and GND pins of the LTC3109 should be designed to minimize voltage drop from stray resistance, and able to carry currents as high as 500 mA . Any small voltage drop in the primary winding conduction path will lower efficiency and increase start-up voltage and capacitor charge time.
Also, due to the low charge currents available at the outputs of the LTC3109, any sources of leakage current on the output voltage pins must be minimized. An example board layout is shown in Figure 4.


Figure 4. Example Component Placement for 2-Layer PC Board (QFN Package). Note That VSTORE and VOUT Capacitor Sizes are Application Dependent

## APPLICATIONS InFORMATION

## DESIGN EXAMPLE 1

This design example will explain how to calculate the necessary reservoir capacitor value for $\mathrm{V}_{\text {OUT }}$ in pulsedload applications, such as a wireless sensor/transmitter. In these types of applications, the load is very small for a majority of the time (while the circuitry is in a low power sleep state), with pulses of load current occurring periodically during a transmit burst.
The reservoir capacitor on $\mathrm{V}_{\text {OUT }}$ supports the load during the transmit pulse; the long sleep time between pulses allows the LTC3109 to accumulate energy and recharge the capacitor (either from the input voltage source or the storage capacitor). A method for calculating the maximum rate at which the load pulses can occur for a given output current from the LTC3109 will also be shown.

In this example, $\mathrm{V}_{\text {OUT }}$ is set to 3.3 V , and the maximum allowed voltage droop during a transmit pulse is $10 \%$, or 0.33 V . The duration of a transmit pulse is 5 ms , with a total average current requirement of 20 mA during the pulse. Given these factors, the minimum required capacitance on $V_{\text {OUT }}$ is:

$$
\mathrm{C}_{\text {OUT }}(\mu \mathrm{F}) \geq \frac{20 \mathrm{~mA} \cdot 5 \mathrm{~ms}}{0.33 \mathrm{~V}}=303 \mu \mathrm{~F}
$$

Note that this equation neglects the effect of capacitor ESR on output voltage droop. For ceramic capacitors and low ESR tantalum capacitors, the ESR will have a negligible effect at these load currents. However, beware of the voltage coefficient of ceramic capacitors, especially those in small case sizes. This greatly reduces the effective capacitance when a DC bias is applied.
A standard value of $330 \mu \mathrm{~F}$ could be used for $\mathrm{C}_{\text {OUT }}$ in this case. Note that the load current is the total current draw on $\mathrm{V}_{\text {OUT }}$, $\mathrm{V}_{\text {OUT2 }}$ and VLDO, since the current for all of these outputs must come from $\mathrm{V}_{\text {OUT }}$ during a pulse. Current contribution from the capacitor on VSTORE is not considered, since it may not be able to recharge between pulses. Also, it is assumed that the harvested charge current from the LTC3109 is negligible compared to the magnitude of the load current during the pulse.

To calculate the maximum rate at which load pulses can occur, you must know how much charge current is available from the LTC3109 $\mathrm{V}_{\text {OUT }}$ pin given the input voltage source being used. This number is best found empirically, since there are many factors affecting the efficiency of the converter. You must also know what the total load current is on $\mathrm{V}_{\text {OUT }}$ during the sleep state (between pulses). Note that this must include any losses, such as storage capacitor leakage.

Let's assume that the charge current available from the LTC3109 is $150 \mu \mathrm{~A}$ and the total current draw on $\mathrm{V}_{\text {OUT }}$ and VLDO in the sleep state is $17 \mu \mathrm{~A}$, including capacitor leakage. We'll also use the value of $330 \mu \mathrm{~F}$ for the $\mathrm{V}_{\text {Out }}$ capacitor. The maximum transmit rate (neglecting the duration of the transmit pulse, which is very short compared to the period) is then given by:

$$
\mathrm{T}=\frac{330 \mu \mathrm{~F} \cdot 0.33 \mathrm{~V}}{150 \mu \mathrm{~A}-17 \mu \mathrm{~A}}=0.82 \mathrm{sec} \text { or } \mathrm{f}_{\mathrm{MAX}}=1.2 \mathrm{~Hz}
$$

Therefore, in this application example, the circuit can support a 5 ms transmit pulse of 20 mA every 0.82 seconds.
It can be seen that for systems that only need to transmit every few seconds (or minutes or hours), the average charge current required is extremely small, as long as the sleep or standby current is low. Even if the available charge current in the example above was only $21 \mu \mathrm{~A}$, if the sleep current was only $5 \mu \mathrm{~A}$, it could still transmit a pulse every seven seconds.
The following formula will allow you to calculate the time it will take to charge the LDO output capacitor and the $V_{\text {OUT }}$ capacitor the first time, from zero volts. Here again, the charge current available from the LTC3109 must be known. For this calculation, it is assumed that the LDO output capacitor is $2.2 \mu \mathrm{~F}$ :

$$
t_{\mathrm{LDO}}=\frac{2.2 \mathrm{~V} \cdot 2.2 \mu \mathrm{~F}}{\mathrm{I}_{\mathrm{CHG}}-\mathrm{I}_{\mathrm{LDO}}}
$$

If there was $150 \mu \mathrm{~A}$ of charge current available and a $5 \mu \mathrm{~A}$ load on the LDO (when the processor is sleeping), the time for the LDO to reach regulation would be only 33 ms .

## LTC3109

## APPLICATIONS IMFORMATION

The time for $\mathrm{V}_{\text {OUT }}$ to charge and reach regulation can be calculated by the formula below, which assumes $\mathrm{V}_{\text {OUT }}$ is programmed to 3.3 V and $\mathrm{C}_{\text {OUT }}$ is $330 \mu \mathrm{~F}$ :

$$
\mathrm{t}_{\text {VOUT }}=\frac{3.3 \mathrm{~V} \cdot 330 \mu \mathrm{~F}}{I_{\mathrm{CHG}}-I_{\text {VOUT }}-I_{\text {LDO }}}+\mathrm{t}_{\mathrm{LDO}}
$$

With $150 \mu \mathrm{~A}$ of charge current available and $5 \mu \mathrm{~A}$ of load on both $\mathrm{V}_{\text {OUT }}$ and VLDO, the time for $\mathrm{V}_{\text {OUT }}$ to reach regulation after the initial application of power would be 7.81 seconds.

## DESIGN EXAMPLE 2

In most pulsed-load applications, the duration, magnitude and frequency of the load current pulses are known and fixed. In these cases, the average charge current required from the LTC3109 to support the average load must be calculated, which can be easily done by the following:

$$
I_{C H G} \geq I_{Q}+\frac{I_{\text {PULSE }} \cdot \mathrm{t}_{\text {PULSE }}}{T}
$$

where $\mathrm{I}_{\mathrm{Q}}$ is the sleep current supplied by $\mathrm{V}_{\text {OUT }}$ and $\mathrm{V}_{\text {LDO }}$ to the external circuitry in-between load pulses, including output capacitor leakage, IPULSE is the total load current during the pulse, tPULSE is the duration of the load pulse and T is the pulse period (essentially the time between load pulses).

In this example, $\mathrm{I}_{Q}$ is $5 \mu \mathrm{~A}$, $\mathrm{I}_{\text {PULSE }}$ is 100 mA , $\mathrm{t}_{\text {PULSE }}$ is 5 ms and $T$ is one hour. The average charge current required from the LTC3109 would be:

$$
\mathrm{I}_{\mathrm{CHG}} \geq 5 \mu \mathrm{~A}+\frac{100 \mathrm{~mA} \cdot 0.005 \mathrm{sec}}{3600 \mathrm{sec}}=5.14 \mu \mathrm{~A}
$$

Therefore, if the LTC3109 has an input voltage that allows it to supply a charge current greater than just $5.14 \mu \mathrm{~A}$, the application can support 100 mA pulses lasting 5 ms every hour. It can be seen that the sleep current of $5 \mu \mathrm{~A}$ is the dominant factor in this example, because the transmit duty cycle is so small $(0.00014 \%)$. Note that for a $V_{\text {OUT }}$ of 3.3 V , the average power required by this application is only $17 \mu \mathrm{~W}$ (not including converter losses).

Keep in mind that the charge current available from the LTC3109 has no effect on the sizing of the $V_{\text {OUT }}$ capacitor, and the $V_{\text {out }}$ capacitor has no effect on the maximum allowed pulse rate.

## TYPICAL APPLICATIONS

Energy Harvester Operates from Small Temperature Differentials of Either Polarity


T1, T2: COILCRAFT LPR6235-752SML

Li-Ion Battery Charger and LDO Operates from a Low Level AC Input


## LTC3109

## TYPICAL APPLICATIONS

Unipolar Energy Harvester Charges Battery Backup


Dual-Input Energy Harvester Generates 5V and 2.2V from Either or Both TEGs, Operating at Different Temperatures of Fixed Polarity

*THE VALUE OF THE COUT CAPACITOR IS DETEMINED BY THE LOAD CHARACTERISTICS

## PACKAGE DESCRIPTION

Please refer to http://www.linear.com/designtools/packaging/ for the most recent package drawings.

## UF Package

20-Lead Plastic QFN ( $4 \mathrm{~mm} \times 4 \mathrm{~mm}$ )
(Reference LTC DWG \# 05-08-1710 Rev A)


NOTE:

1. DRAWING IS PROPOSED TO BE MADE A JEDEC PACKAGE OUTLINE MO-220

VARIATION (WGGD-1)—TO BE APPROVED
2. DRAWING NOT TO SCALE
3. ALL DIMENSIONS ARE IN MILLIMETERS
4. DIMENSIONS OF EXPOSED PAD ON BOTTOM OF PACKAGE DO NOT INCLUDE

MOLD FLASH. MOLD FLASH, IF PRESENT, SHALL NOT EXCEED 0.15 mm ON ANY SIDE
5. EXPOSED PAD SHALL BE SOLDER PLATED
6. SHADED AREA IS ONLY A REFERENCE FOR PIN 1 LOCATION

ON THE TOP AND BOTTOM OF PACKAGE

## PACKAGE DESCRIPTION

Please refer to http://www.linear.com/designtools/packaging/ for the most recent package drawings.

## GN Package

20-Lead Plastic SSOP (Narrow . 150 Inch)
(Reference LTC DWG \# 05-08-1641 Rev B)


RECOMMENDED SOLDER PAD LAYOUT


1. CONTROLLING DIMENSION: INCHES
2. DIMENSIONS ARE IN $\frac{\text { INCHES }}{\text { (MILLIMETERS) }}$
3. DRAWING NOT TO SCALE
4. PIN 1 CAN BE BEVEL EDGE OR A DIMPLE
*DIMENSION DOES NOT INCLUDE MOLD FLASH. MOLD FLASH SHALL NOT EXCEED 0.006 " ( 0.152 mm ) PER SIDE
**DIMENSION DOES NOT INCLUDE INTERLEAD FLASH. INTERLEAD FLASH SHALL NOT EXCEED 0.010" ( 0.254 mm ) PER SIDE

## REVISION HISTORY

| REV | DATE | DESCRIPTION | PAGE NUMBER |
| :---: | :---: | :--- | :---: |
| A | $06 / 12$ | Added vendor Information to Table 5 | 15 |
| B | $08 / 13$ | Changed Würth transformer part numbers | 15 |

## LTC3109

## TYPICAL APPLICATION

Unipolar TEG Energy Harvester for Low Resistance/High Current Inputs, Using External Charge Pump Rectifiers



Efficiency vs $\mathrm{V}_{\mathrm{IN}}$


## RELATED PARTS

| PART NUMBER | DESCRIPTION | COMMENTS |
| :---: | :---: | :---: |
| $\begin{aligned} & \text { LTC3108/ } \\ & \text { LTC3108-1 } \end{aligned}$ | Ultralow Voltage Step-Up Converter and Power Manager | $\mathrm{V}_{\text {IN: }}: 0.02 \mathrm{~V}$ to $1 \mathrm{~V}, \mathrm{~V}_{\text {OUT }}=2.2 \mathrm{~V}, 2.35 \mathrm{~V}, 3.3 \mathrm{~V}, 4.1 \mathrm{~V}, 5 \mathrm{~V}, \mathrm{I}_{\mathrm{Q}}=6 \mu \mathrm{~A}$, $4 \mathrm{~mm} \times 3 \mathrm{~mm}$ DFN-12, SSOP-16; LTC3108-1 $\mathrm{V}_{\text {OUT }}=2.2 \mathrm{~V}, 2.5 \mathrm{~V}, 3 \mathrm{~V}, 3.7 \mathrm{~V}, 4.5 \mathrm{~V}$ |
| LTC4070 | Micropower Shunt Battery Charger | $1 \%$ Float Voltage Accuracy, 50 mA Max Shunt Current, $\mathrm{V}_{\text {OUT }}=4.0 \mathrm{~V}, 4.1 \mathrm{~V}, 4.2 \mathrm{~V}$, $\mathrm{I}_{\mathrm{O}}=450 \mathrm{nA}, 2 \mathrm{~mm} \times 3 \mathrm{~mm}$ DFN- $-\mathrm{MSOP}-8$ |
| LTC1041 | Bang-Bang Controller | $\mathrm{V}_{\text {IN }}: 2.8 \mathrm{~V}$ to 16V; $\mathrm{V}_{\text {OUT(MIN) }}=\mathrm{Adj} ; \mathrm{I}_{\mathrm{Q}}=1.2 \mathrm{~mA} ; \mathrm{I}_{\text {SD }}<1 \mu \mathrm{~A} ; ~$ S0-8 Package |
| LTC1389 | Nanopower Precision Shunt Voltage Reference | $\mathrm{V}_{\text {OUT(MIN }}=1.25 \mathrm{~V} ; \mathrm{I}_{\mathrm{Q}}=0.84 \mathrm{~A} ;$ S0-8 Package |
| $\begin{aligned} & \text { LT1672/LT1673/ } \\ & \text { TT1674 } \end{aligned}$ | Single-/Dual-/Quad-Precision $2 \mu$ A Rail-to-Rail Op Amps | SO-8, SO-14 and MSOP-8 Packages |
| LT3009 | $3 \mu \mathrm{~A} \mathrm{I}_{\mathrm{Q}}, 20 \mathrm{~mA}$ Linear Regulator | $\mathrm{V}_{\text {In: }} 1.6 \mathrm{~V}$ to 20 V ; $\mathrm{V}_{\text {OUT(MIN): }}$ : 0.6 V to $\mathrm{Adj}, 1.2 \mathrm{~V}, 1.5 \mathrm{~V}, 1.8 \mathrm{~V}, 2.5 \mathrm{~V}, 3.3 \mathrm{~V}$, 5 V to Fixed; $\mathrm{I}_{\mathrm{Q}}=3 \mu \mathrm{~A} ; I_{\mathrm{SD}}<1 \mu \mathrm{~A} ; 2 \mathrm{~mm} \times 2 \mathrm{~mm}$ DFN-8 and SC70 Packages |
| LTC3588-1 | Piezoelectric Energy Generator with Integrated High Efficiency Buck Converter | $\mathrm{V}_{\text {IN: }}$ : 2.7 V to 20V; $\mathrm{V}_{\text {OUT(MIN): }}$ : Fixed to $1.8 \mathrm{~V}, 2.5 \mathrm{~V}, 3.3 \mathrm{~V}, 3.6 \mathrm{~V} ; \mathrm{I}_{\mathrm{Q}}=0.95 \mathrm{HA}$; $3 \mathrm{~mm} \times 3 \mathrm{~mm}$ DFN-10 and MSOP-10E Packages |
| LT8410/LT8410-1 | Micropower 25mA/8mA Low Noise Boost Converter with Integrated Schottky Diode and Output Disconnect | $\mathrm{V}_{\text {IN: }}: 2.6 \mathrm{~V}$ to $16 \mathrm{~V} ; \mathrm{V}_{\text {OUT(MIN) }}=40 \mathrm{~V}_{\text {MAX }} ; \mathrm{I}_{\mathrm{Q}}=8.5 \mu \mathrm{~A} ; \mathrm{I}_{\mathrm{SD}}<1 \mu \mathrm{~A}$; $2 \mathrm{~mm} \times 2 \mathrm{~mm}$ DFN-8 Package |

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[^0]:    1 http://www.linear.com

[^1]:    $2^{\text {http://www.altium.com/altium-designer/overview }}$

[^2]:    ${ }^{1}$ All results about simulation will be describe in next chapter.
    ${ }^{2}$ Data sheet LTC3108 is in the Appendix B.

[^3]:    ${ }^{3}$ Values of the homemade coil will be describe in next chapter

[^4]:    ${ }^{4}$ Data sheet LTC3109 is in the Appendix C

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    *Patent pending.

